

EESM-log-AR:

An Efficient Error Model for OFDM MIMO Systems over Time-Varying Channels

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Fundamentals of Networking Lab

2021 Workshop on ns-3

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Outline

- 1. Motivation:** Fast ns-3 error models for increasingly complex Wi-Fi physical layer scenarios
- 2. Approach:** Take link-to-system mapping approach a step further
 - **EESM-log-AR** based error model for ns-3
- 3. Results:** A link-to-system mapping with **constant run-time** and **modest storage requirement**

What Is an Error Model?

- An error model represents packet error rate (PER) as a function of

Channel type

MCS

Bandwidth

MIMO
dimension

RX SNR

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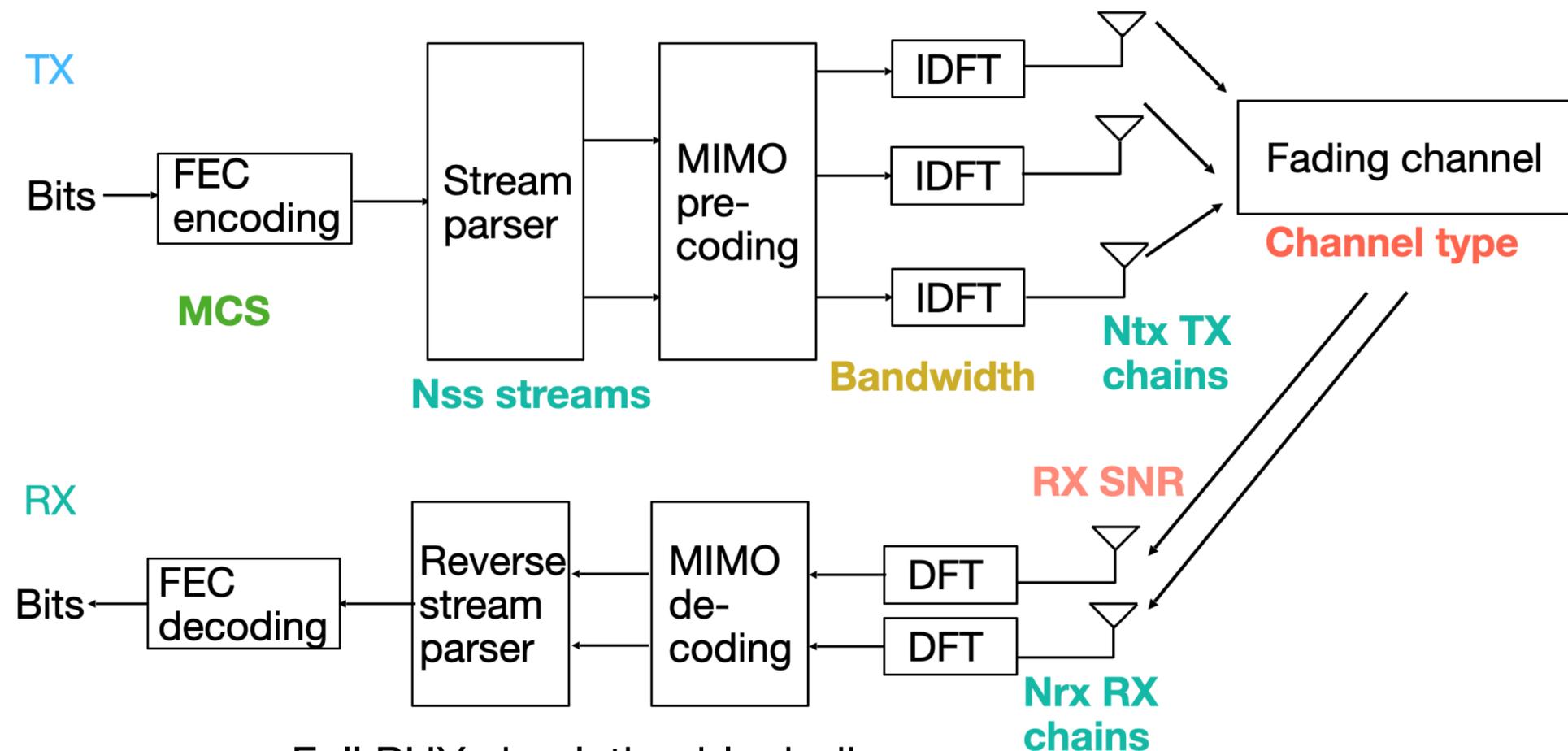
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Full PHY simulation block diagram

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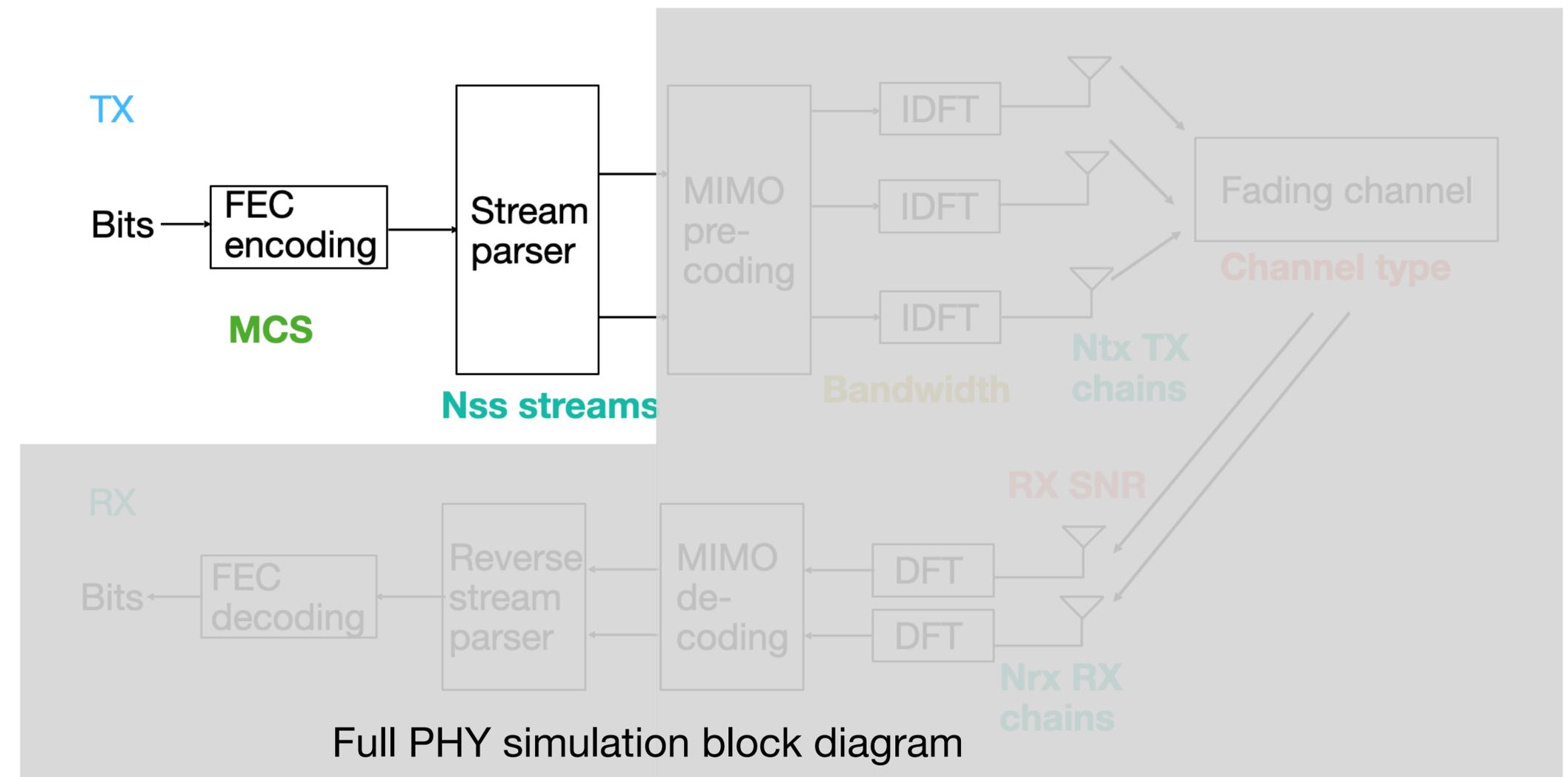
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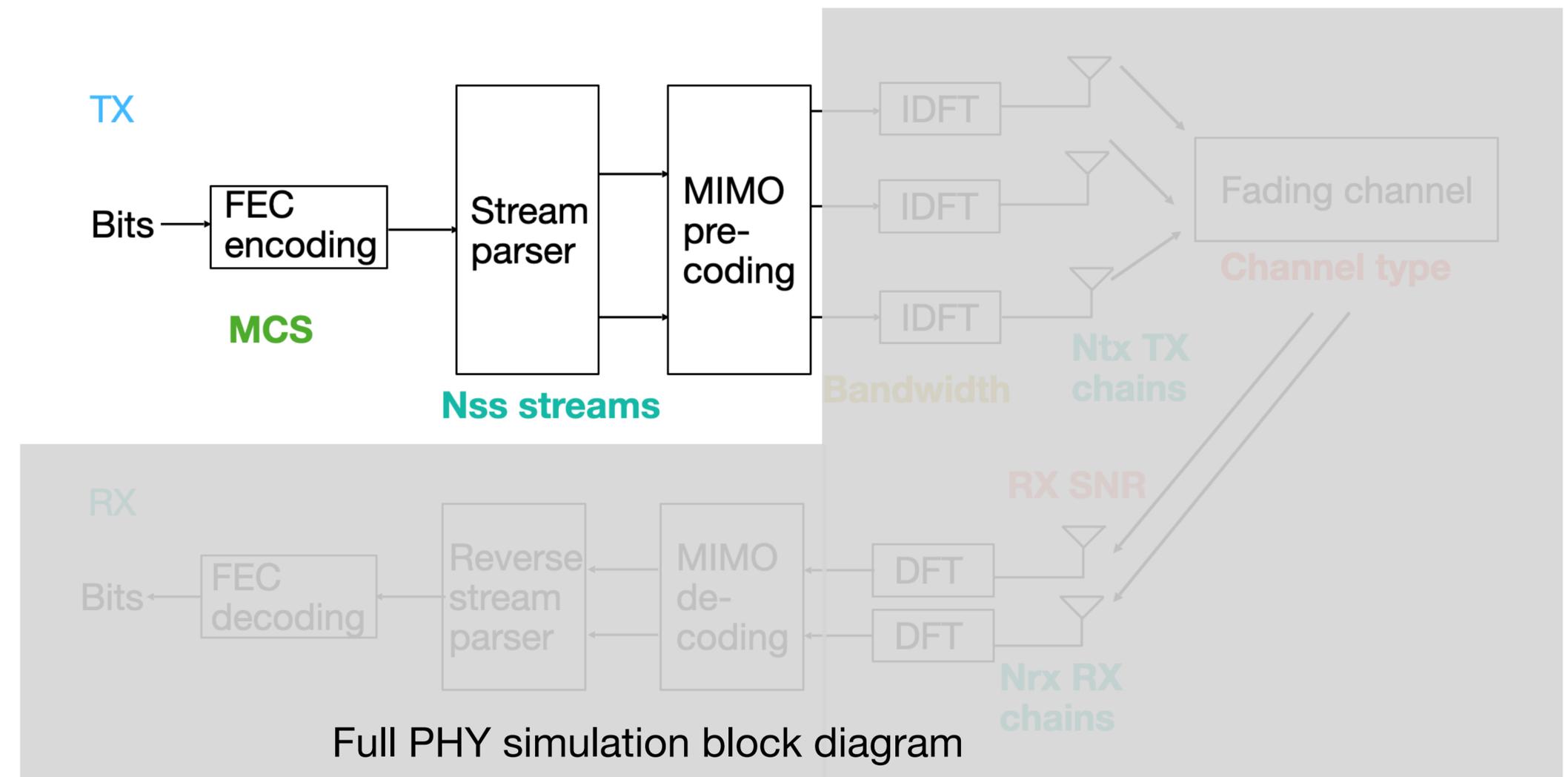
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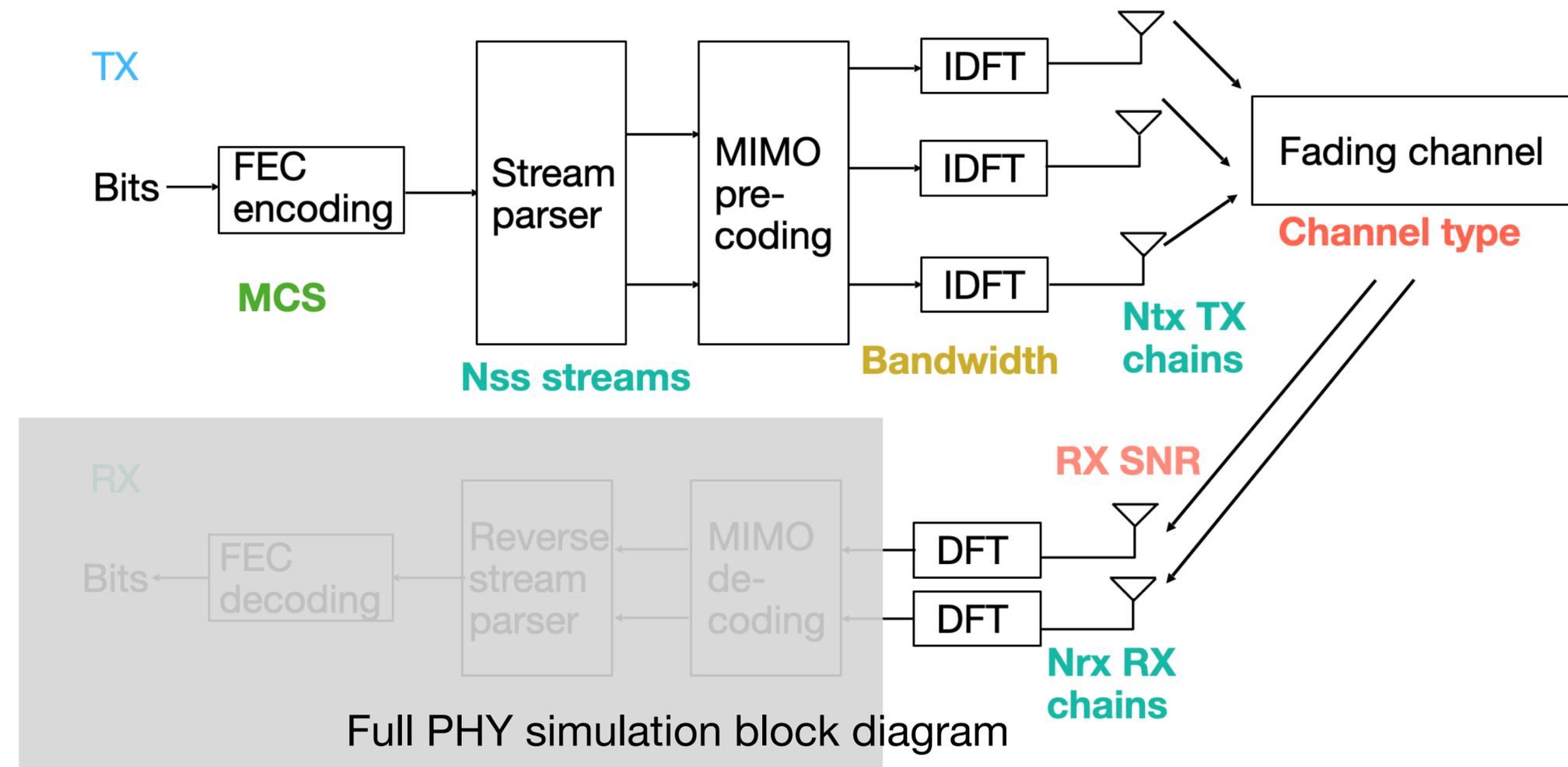
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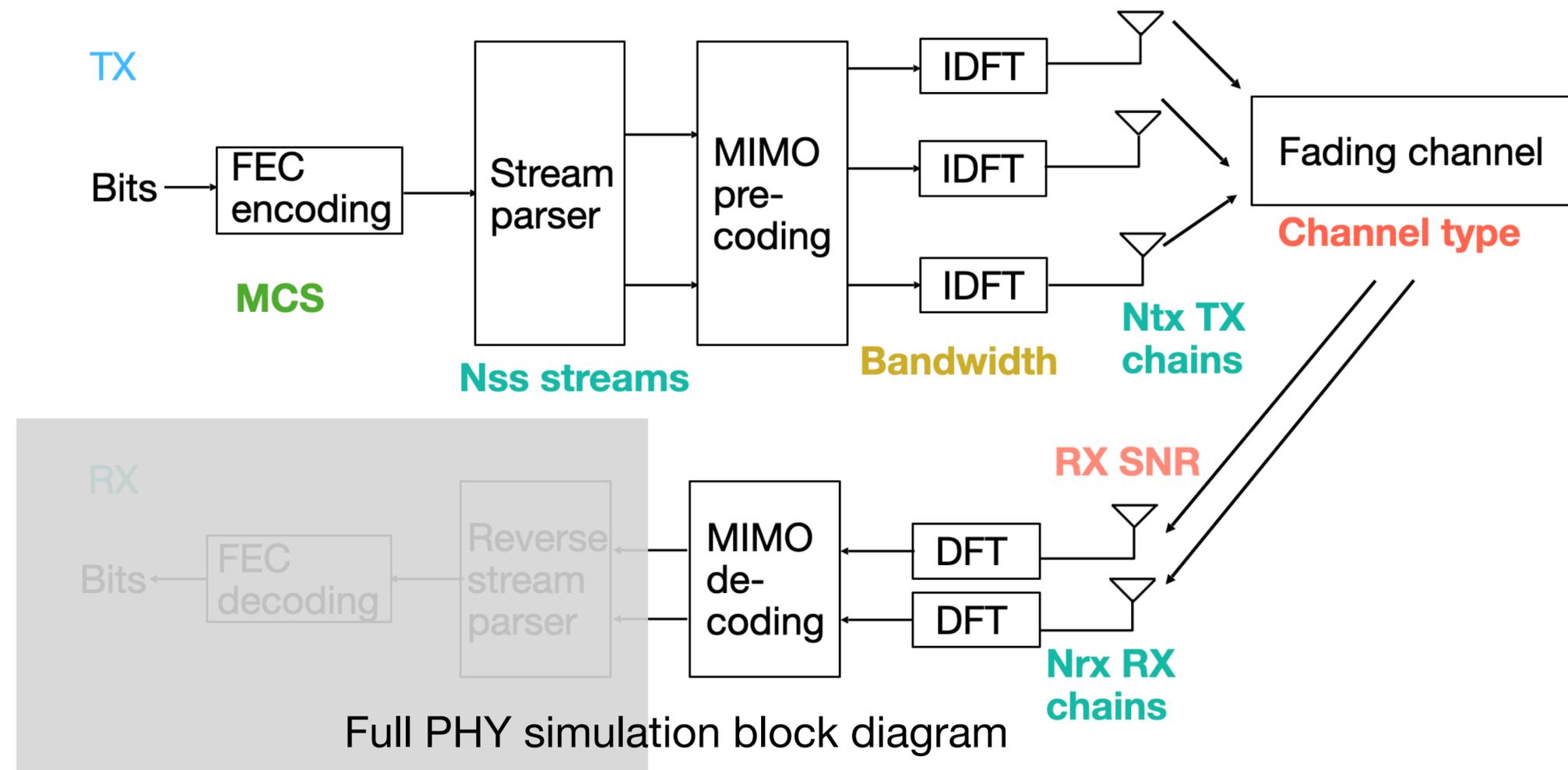
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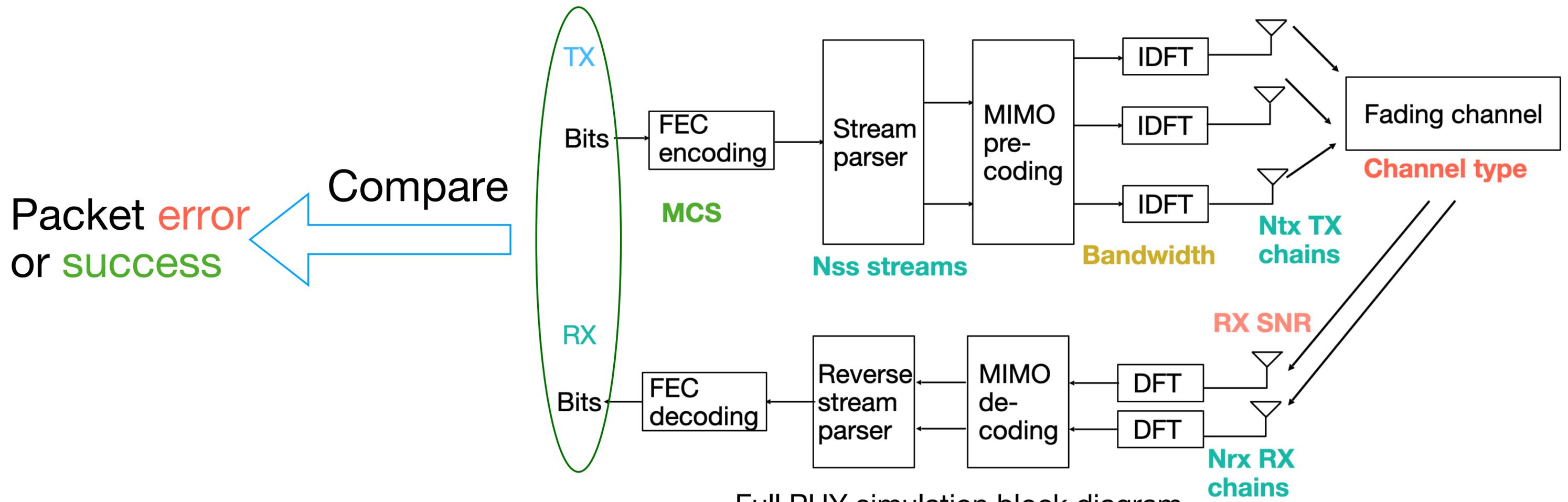
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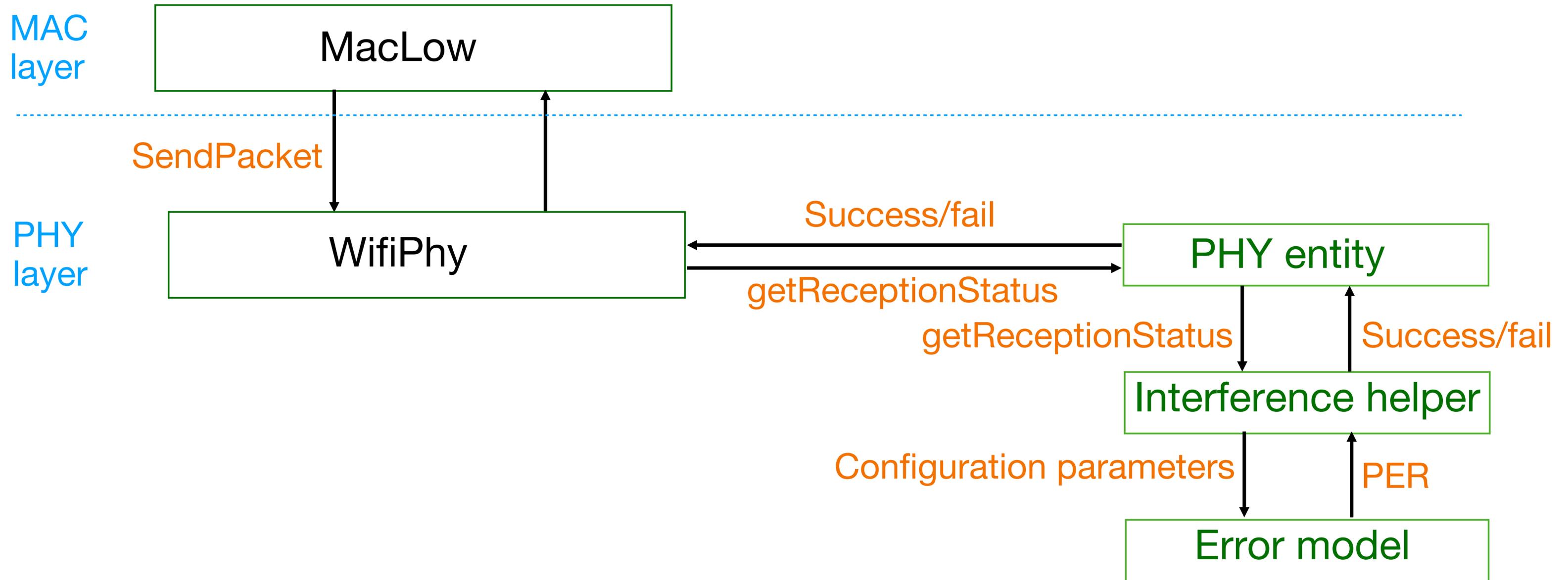
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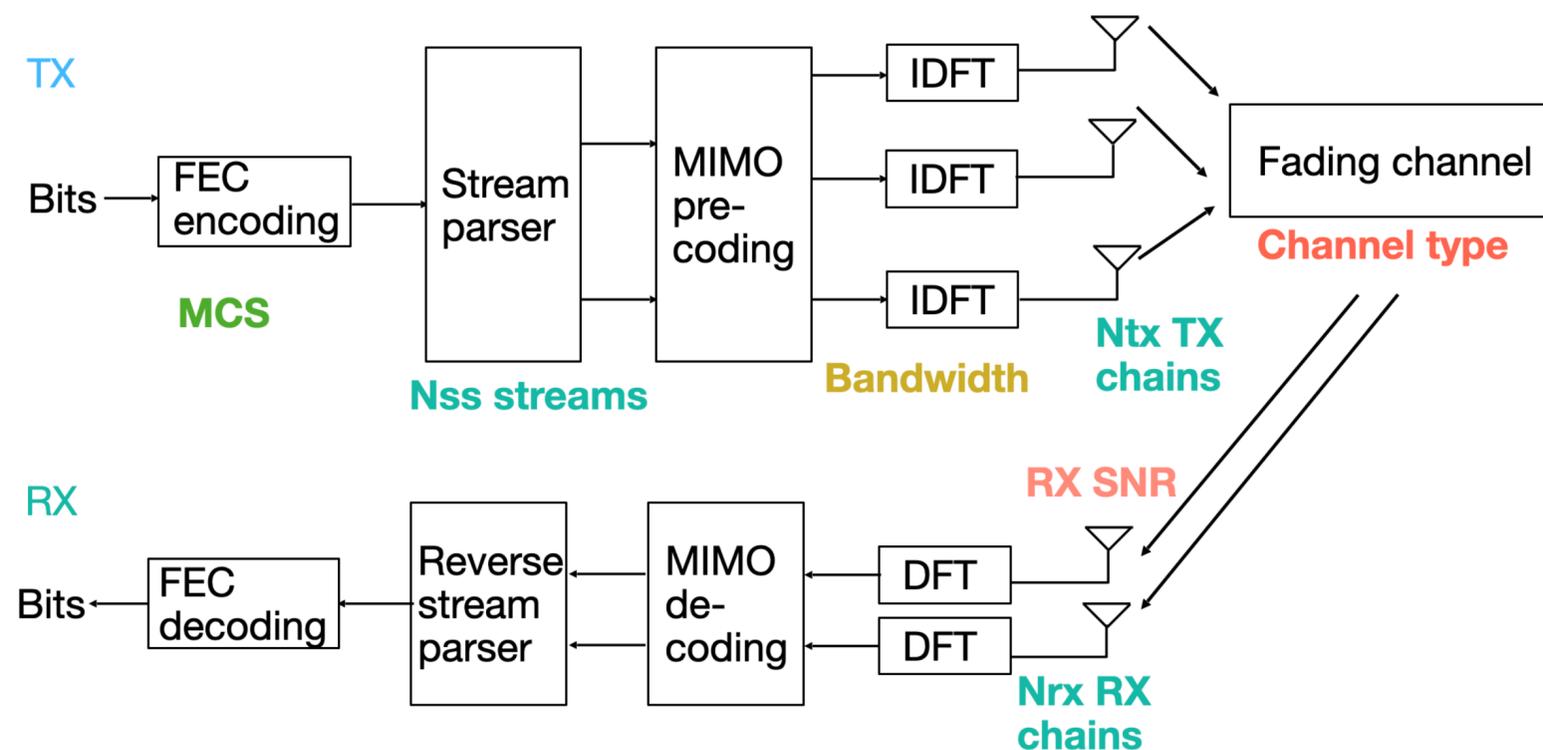
What Is an Error Model?



ns-3 WifiNetDevice example

Why Need an Efficient Error Model?

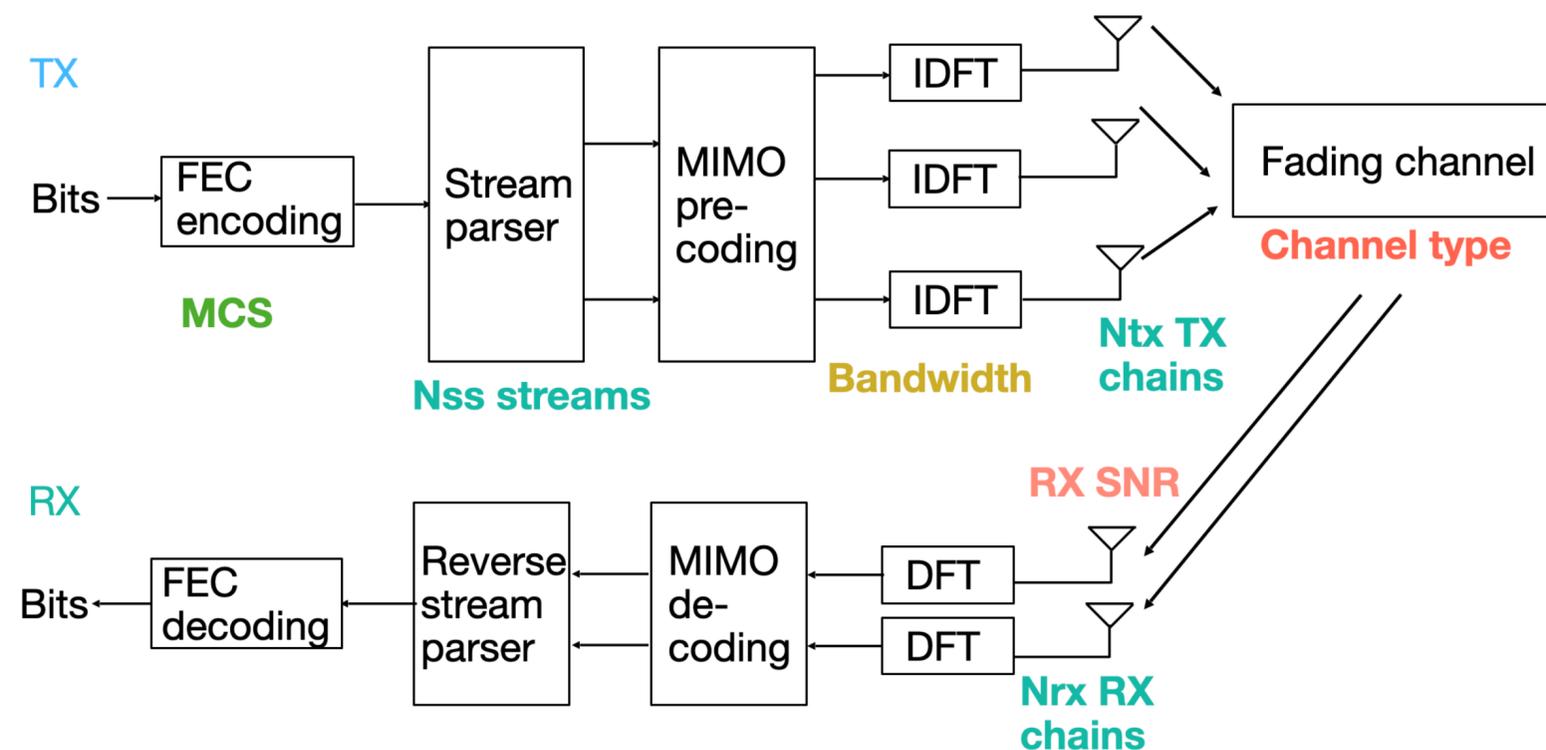
- Full PHY model is the most accurate error model



Full PHY simulation block diagram

Why Need an Efficient Error Model?

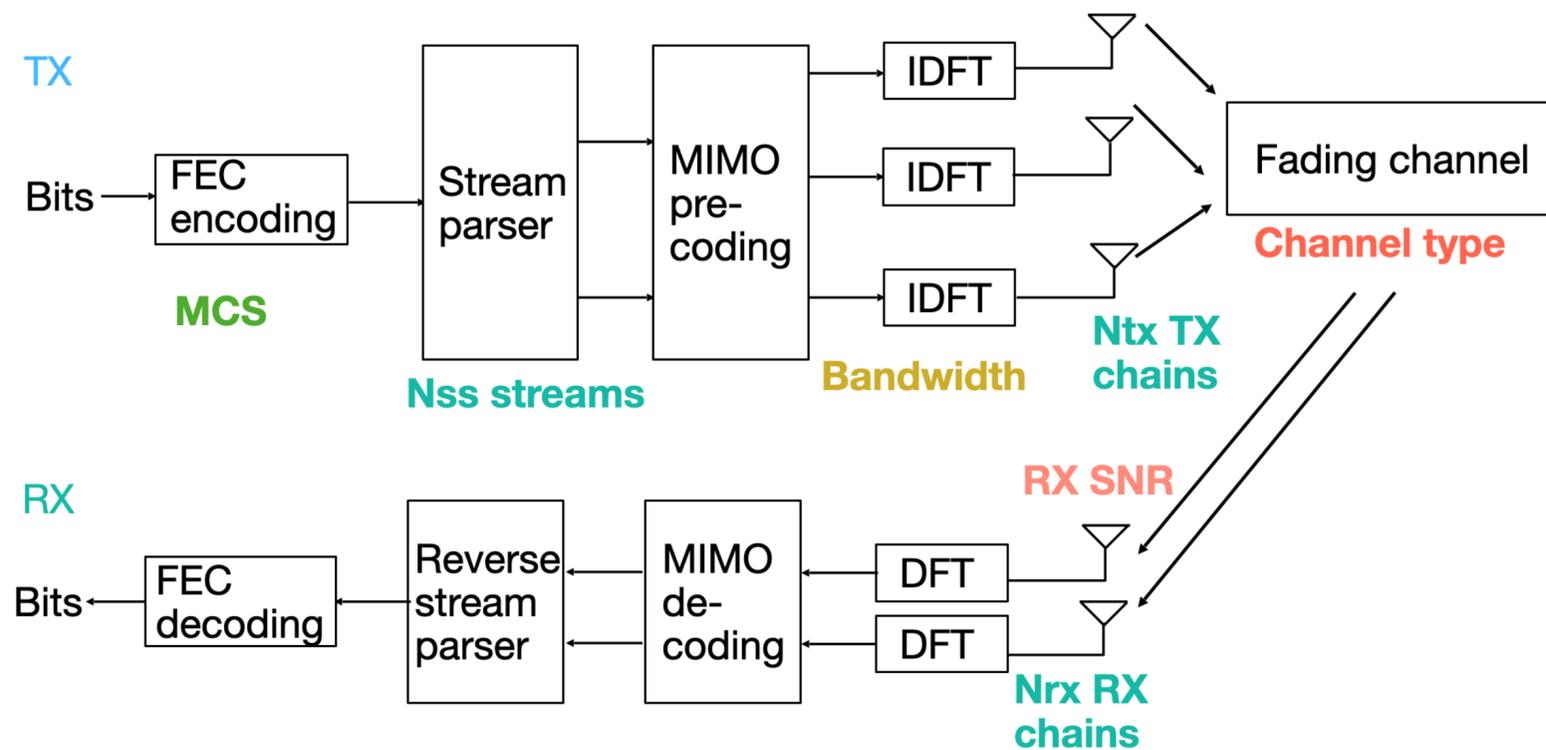
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- However, full PHY simulation is **prohibitively slow** for a cross-layer simulator



Full PHY simulation block diagram

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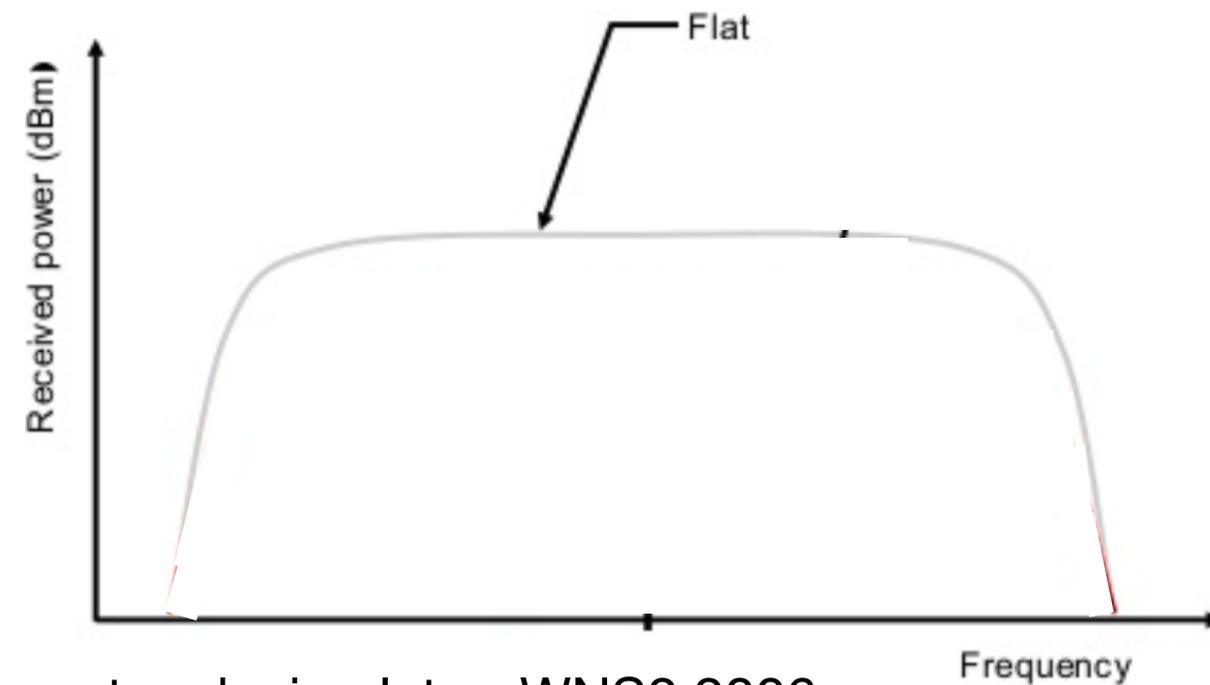
Runtime of single link 200,000-packet simulation (Table 1)

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History of ns-3 Error Models

YANS model

- Original ns-3 Wi-Fi PHY is based on OFDM, SISO, **frequency-flat additive white Gaussian noise (AWGN)** channel, and can be **easily computed**

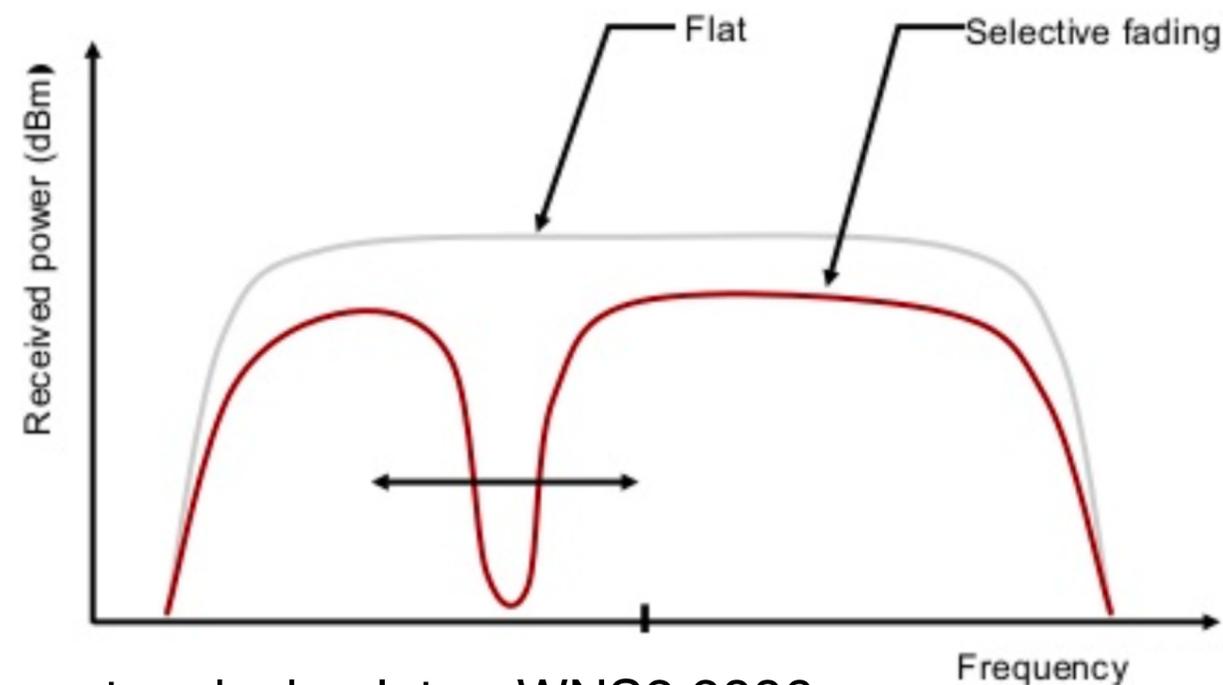


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YANS model

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- However, **frequently-selective fading channels** commonly occur in OFDM system, and this greatly impacts system performance

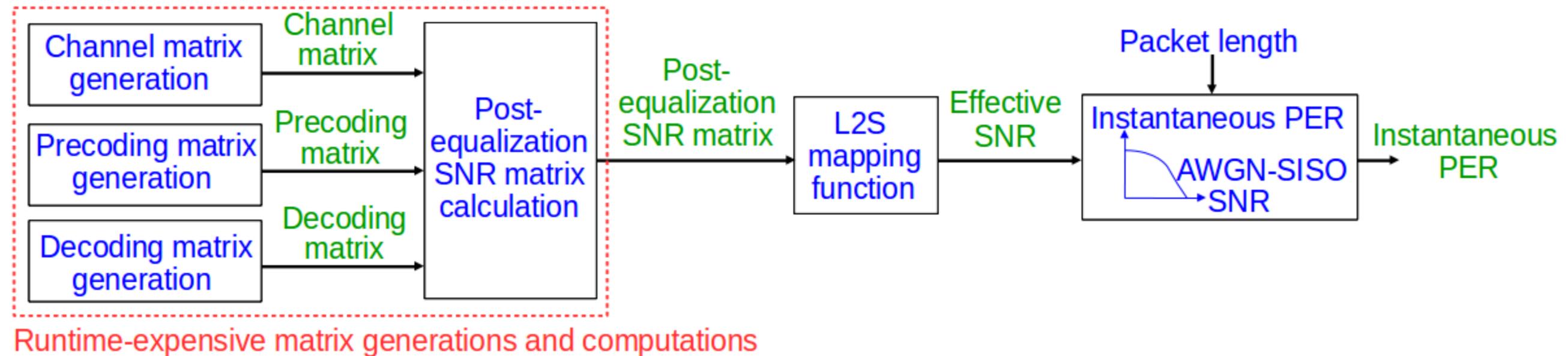


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Link-to-system (L2S) mapping

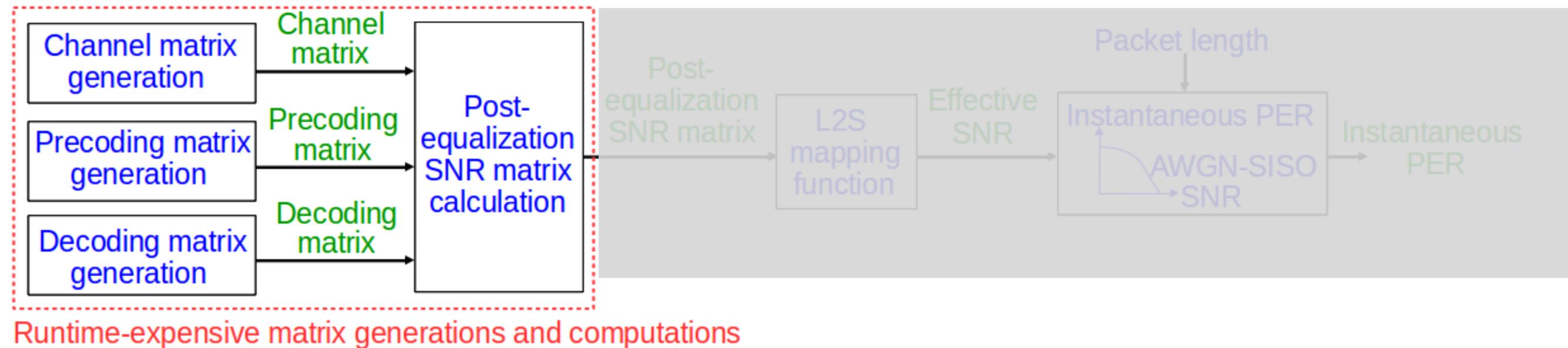
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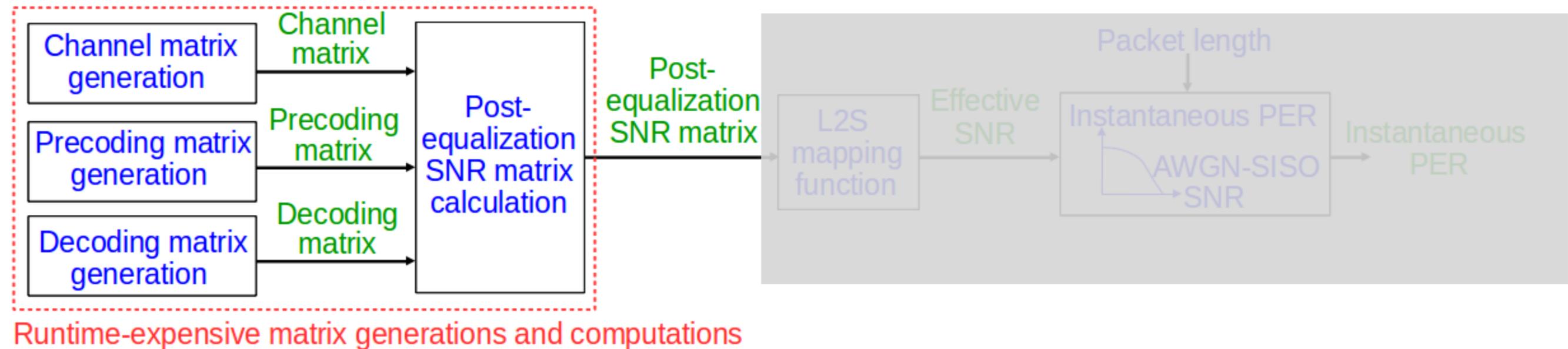
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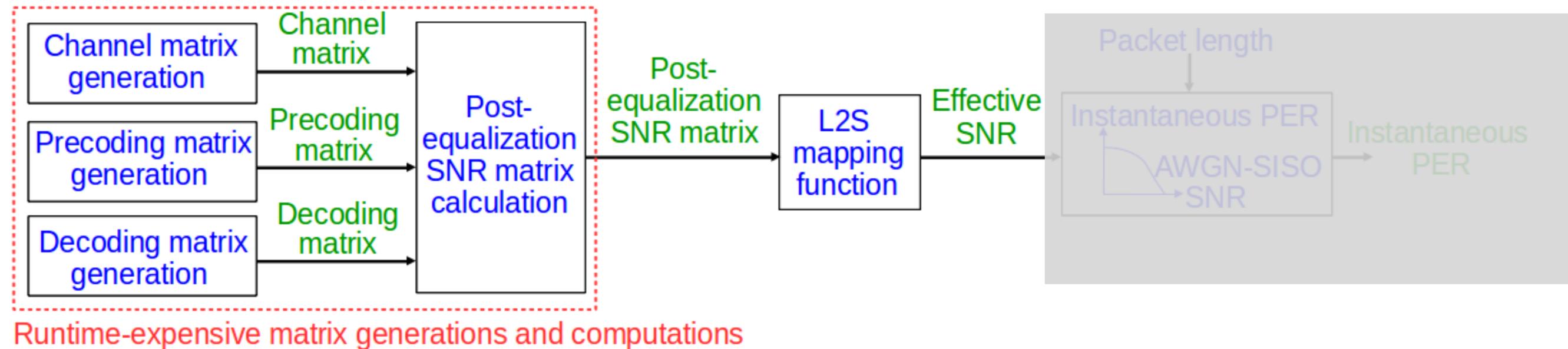
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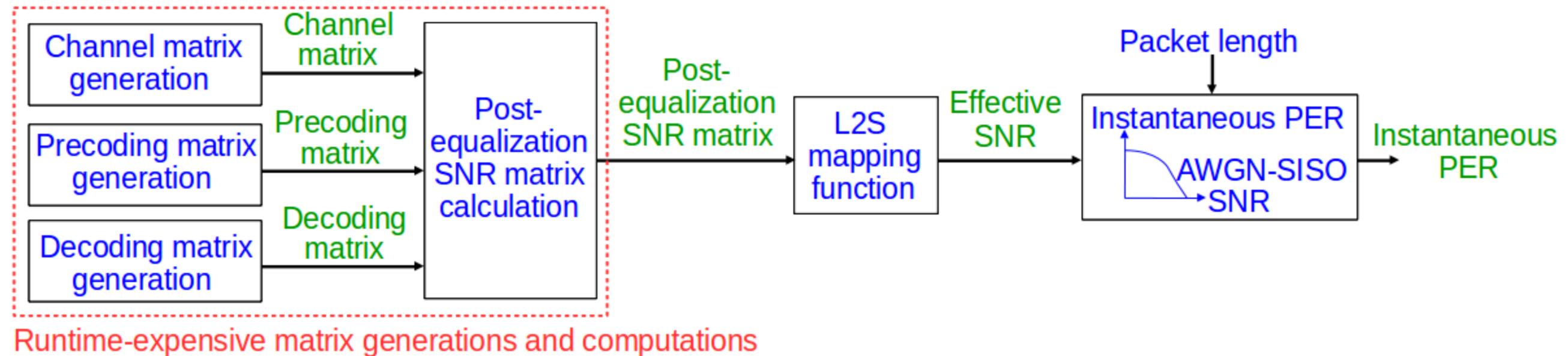
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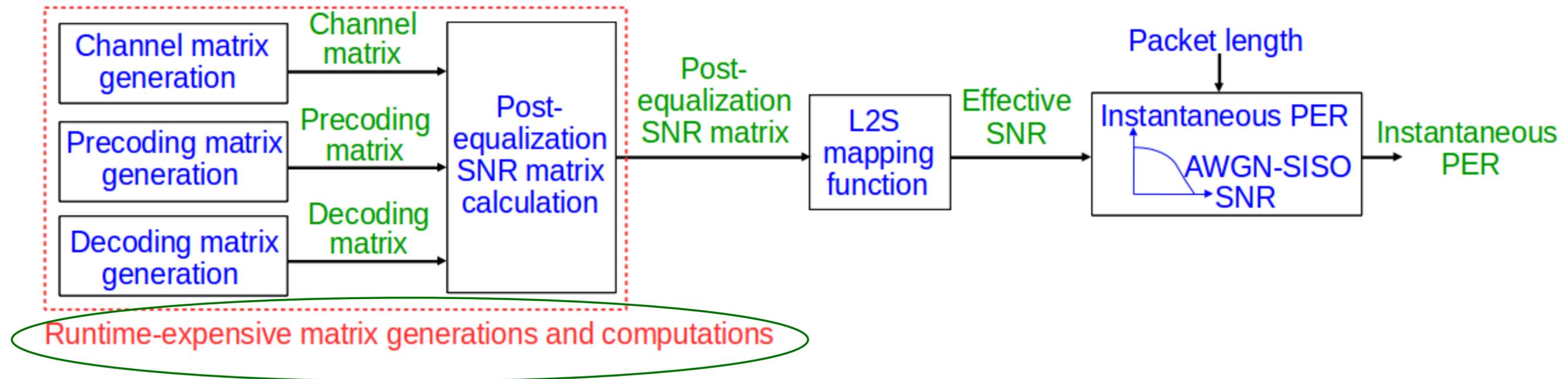
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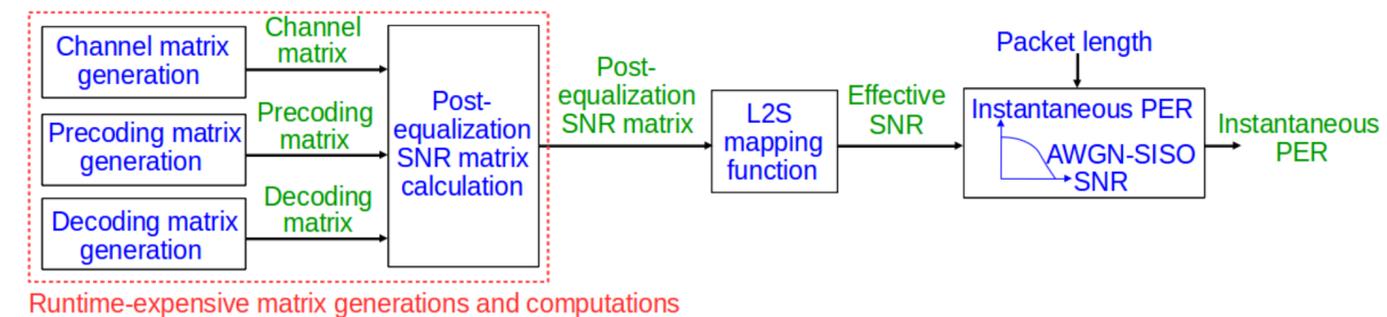
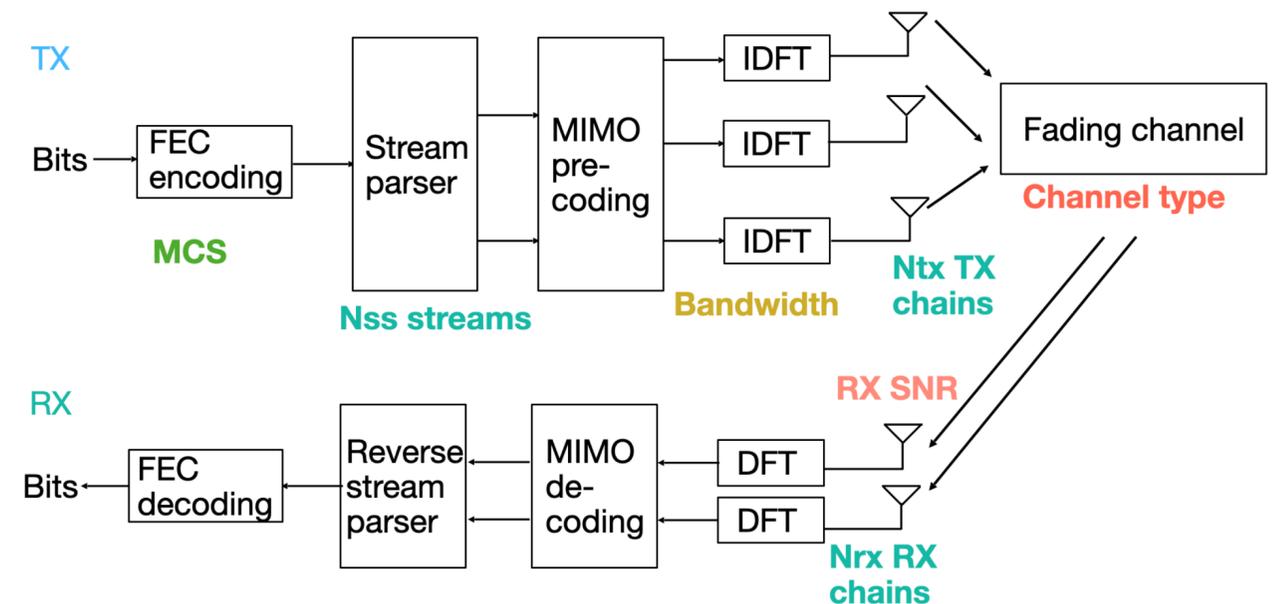
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Full PHY:

L2S mapping:



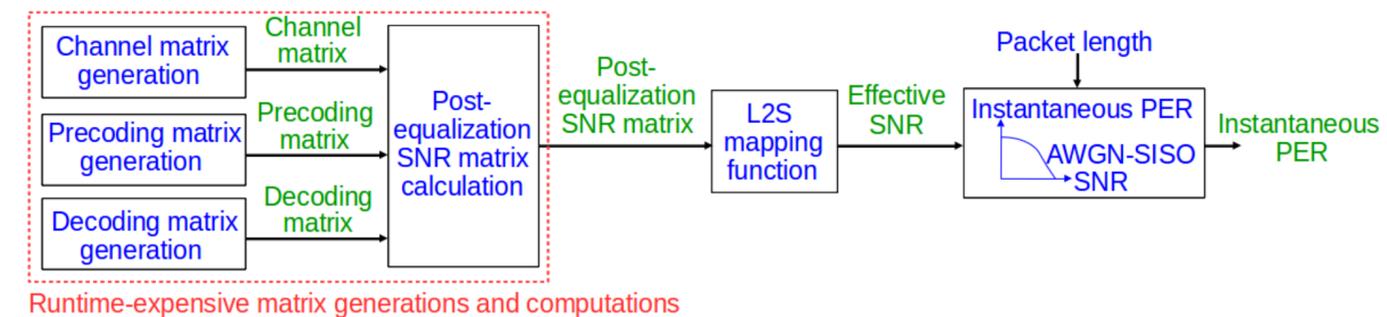
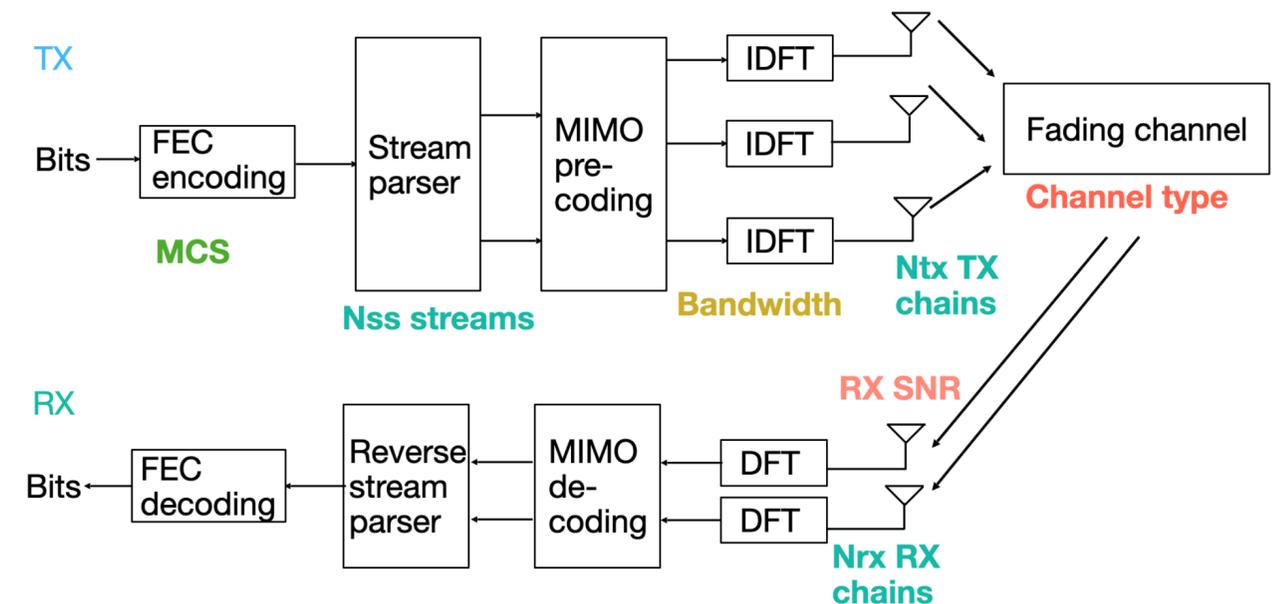
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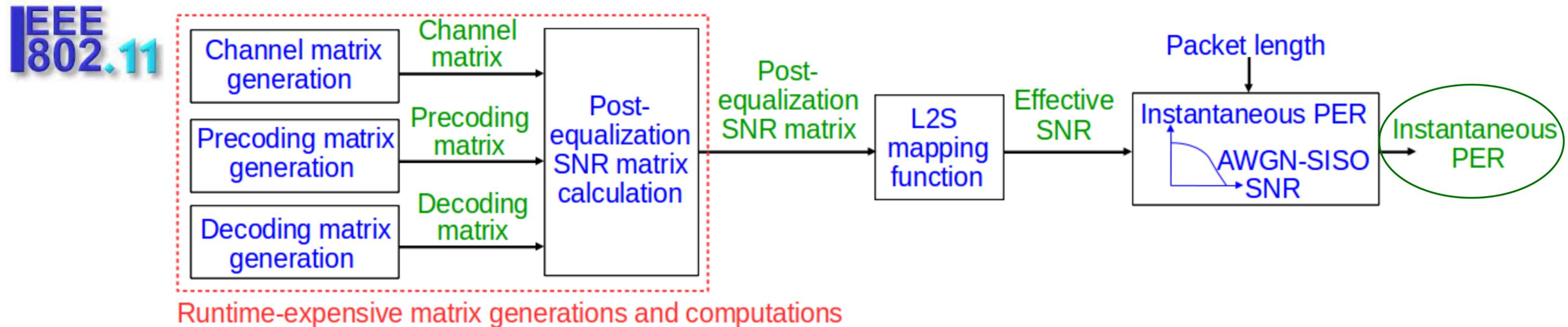
L2S mapping:



How to reduce runtime when simulating complex PHY?

Key Observation

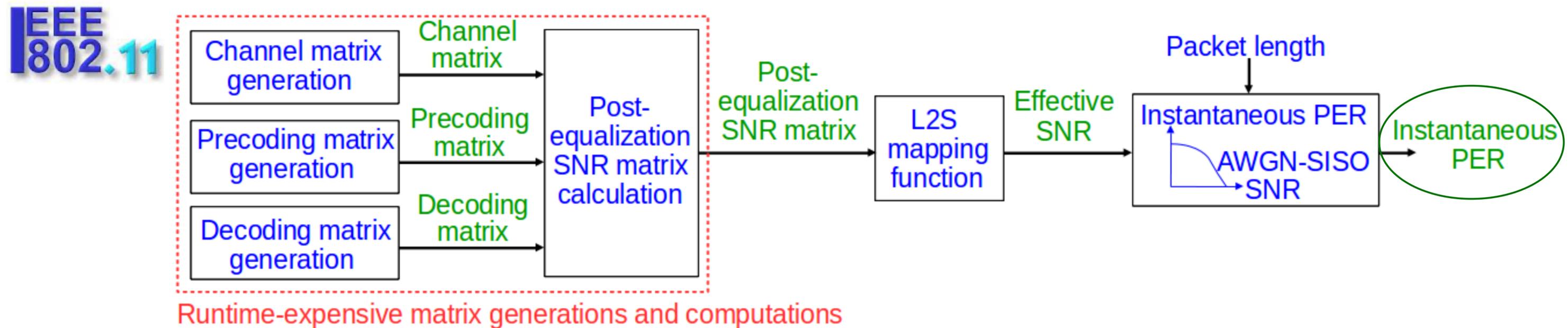
L2S mapping suggested by IEEE TGax group:



Observation: upper layer only needs instantaneous PER (random process)

Key Observation

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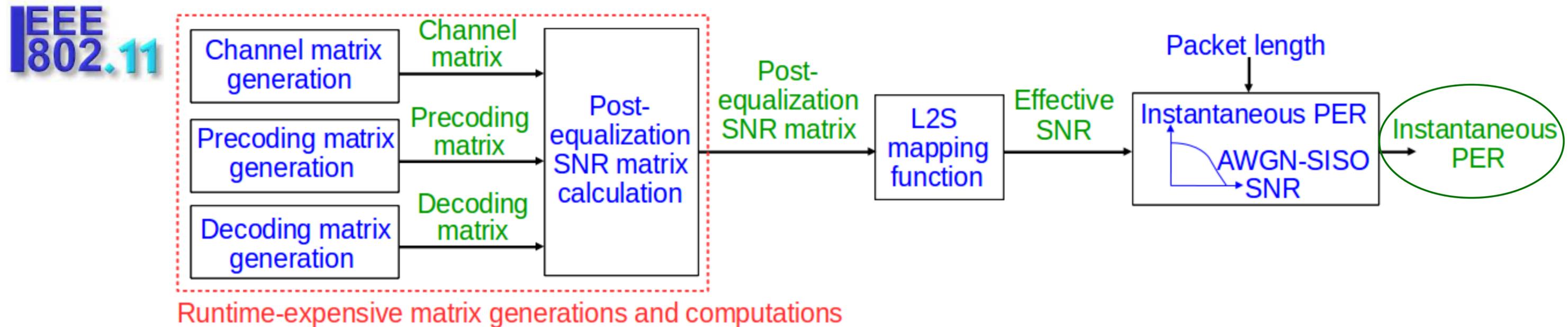


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Q1: Can we **bypass** runtime-expensive matrix calculation and **directly store average PER** (mean of instantaneous PER)?

Key Observation

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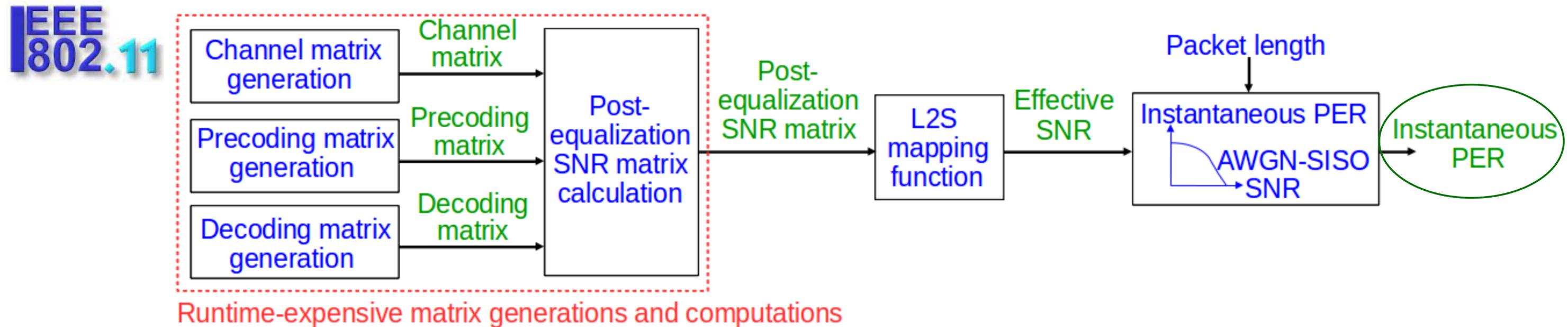
Q1: Can we **bypass** runtime-expensive matrix calculation and **directly store average PER (mean of instantaneous PER)**?



No variance, skewness, kurtosis, time correlation information

Key Observation

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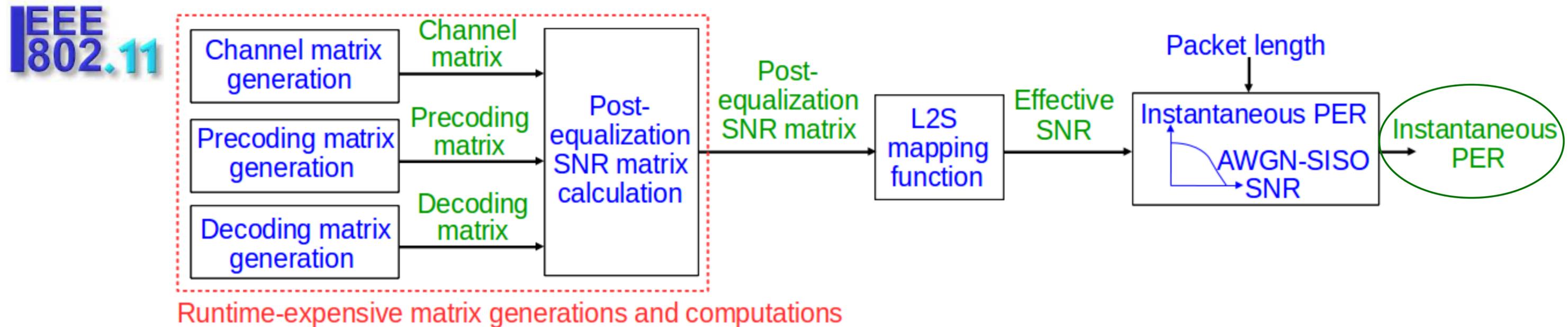


Observation: upper layer only needs instantaneous PER (random process)

Q2: Can we **bypass** runtime-expensive matrix calculation and **directly model instantaneous PER**?

Key Observation

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Q2: Can we **bypass** runtime-expensive matrix calculation and **directly model instantaneous PER**?

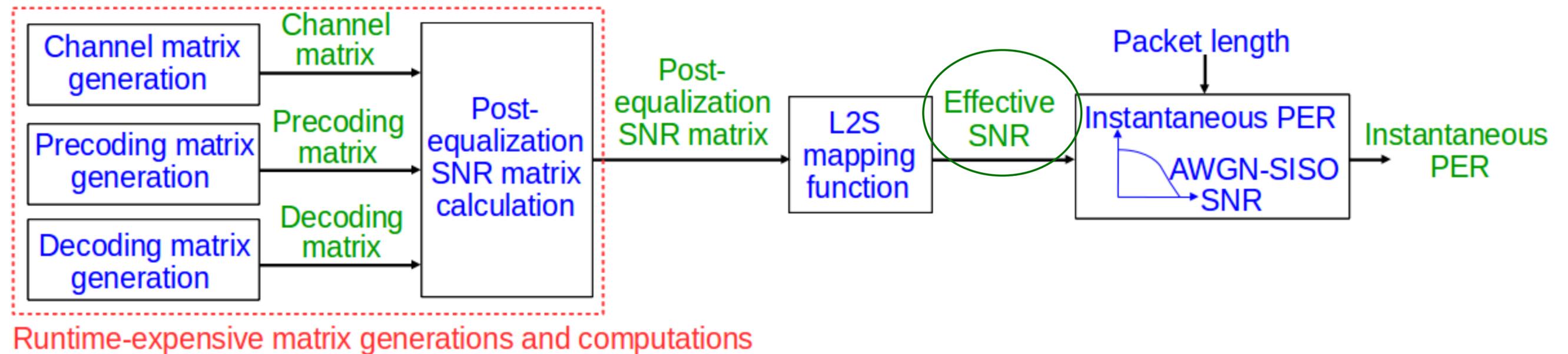


Cannot provide models of instantaneous PERs for different packet lengths

Key Observation

L2S mapping suggested by IEEE TGax group:

IEEE
802.11



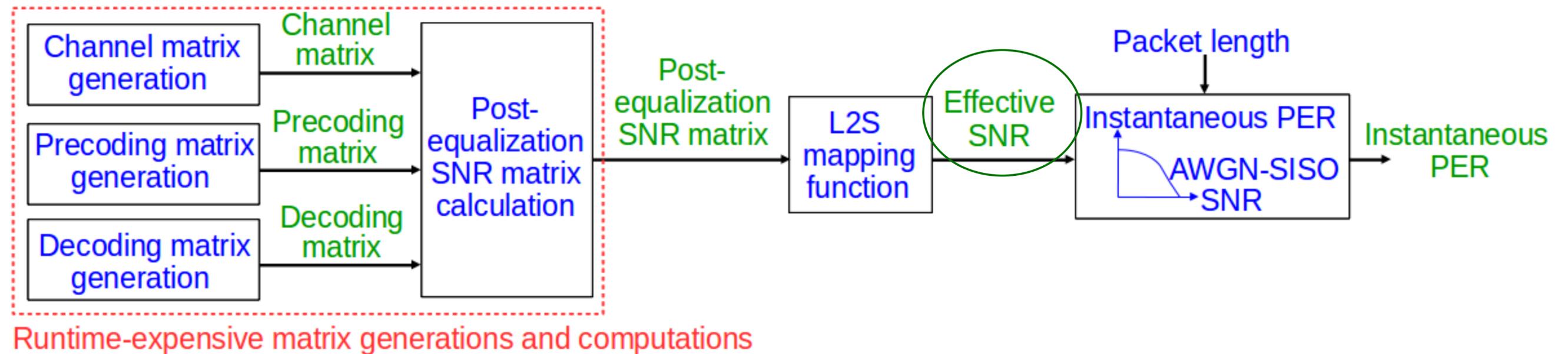
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Q3: Can we **bypass** runtime-expensive matrix calculation and **directly model effective SNR**?

Key Observation

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Observation: upper layer only needs instantaneous PER (random process)

Q3: Can we **bypass** runtime-expensive matrix calculation and **directly model effective SNR**?

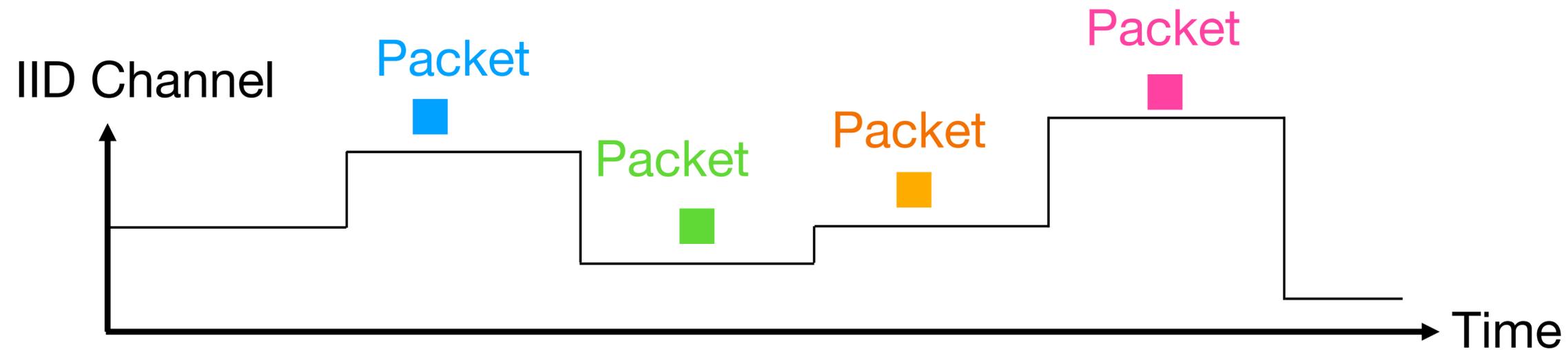


Effective SNR is insensitive to packet length and is easy to be mapped into instantaneous PER

New Method: EESM-log-SGN

Previous State-of-the-art

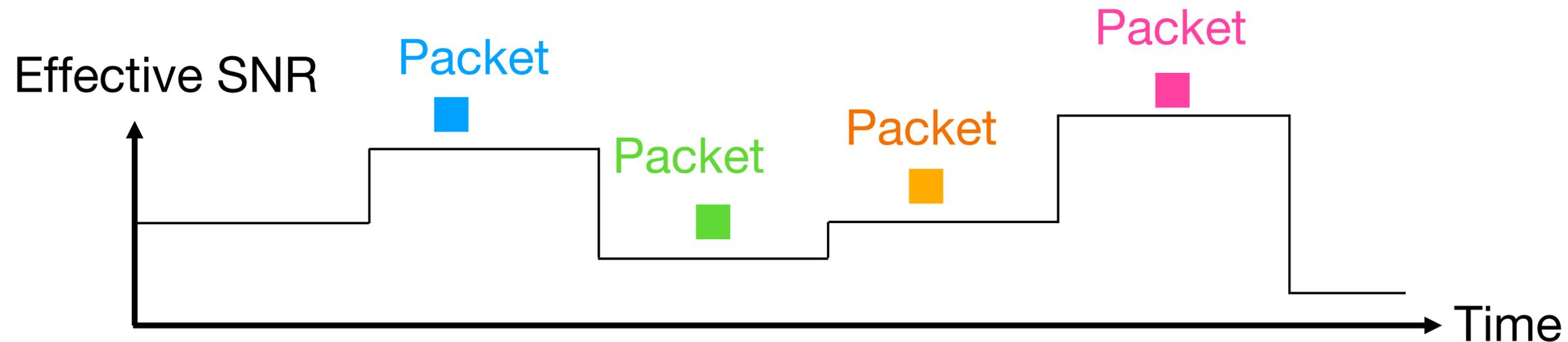
Assume IID channel for different packets



New Method: EESM-log-SGN

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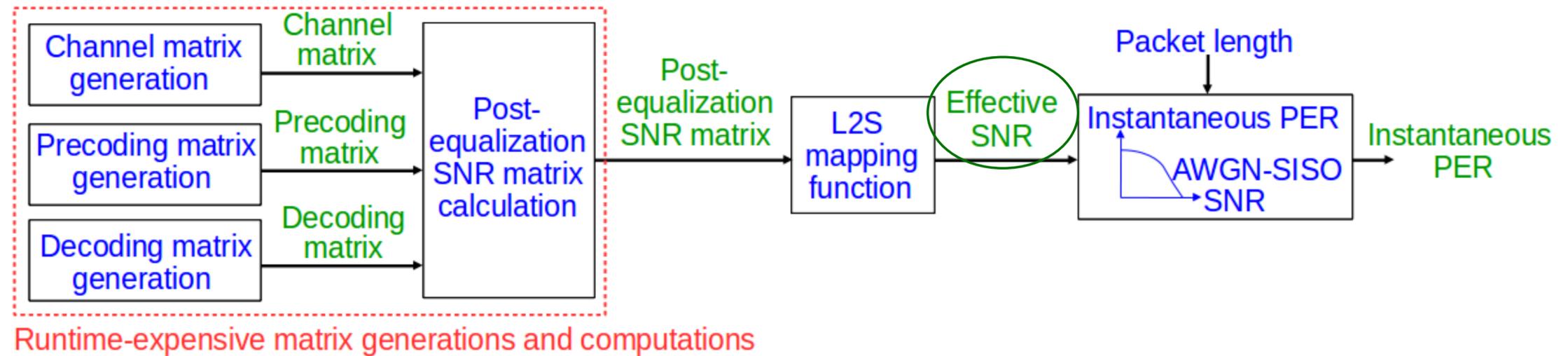
Assume IID channel for different packets, then effective SNR for different packets are also IID



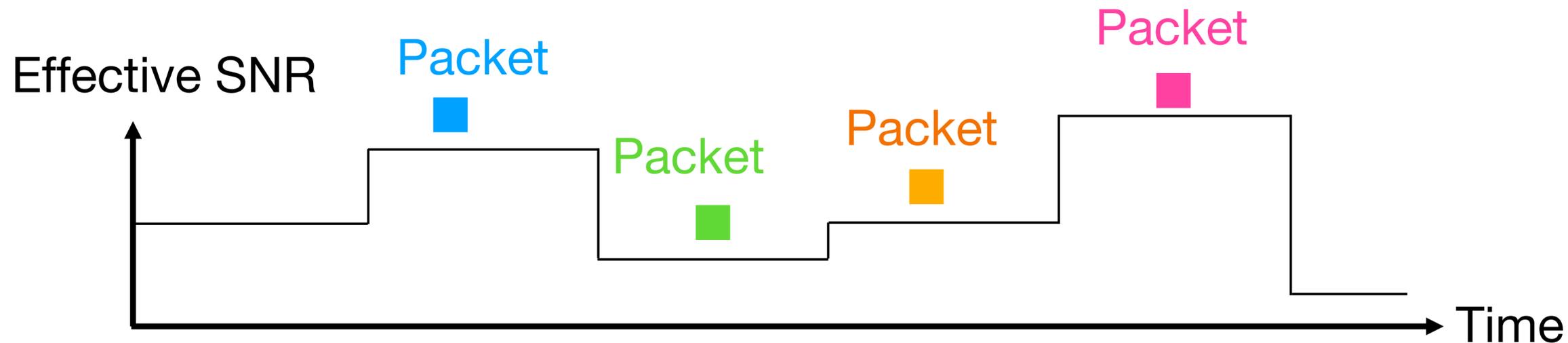
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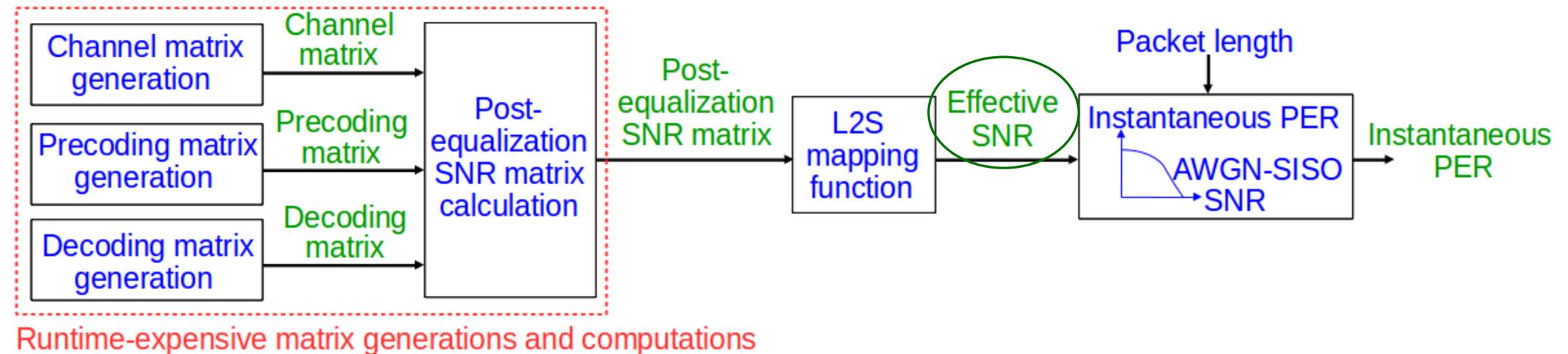
Assume IID channel, model effective SNR distribution, and directly outputs IID effective SNRs



New Method: EESM-log-SGN

Previous State-of-the-art

L2S mapping:



Under IID channel & EESM L2S mapping function, effective SNR distribution follows:

Log-skew generalized normal (log-SGN) distribution

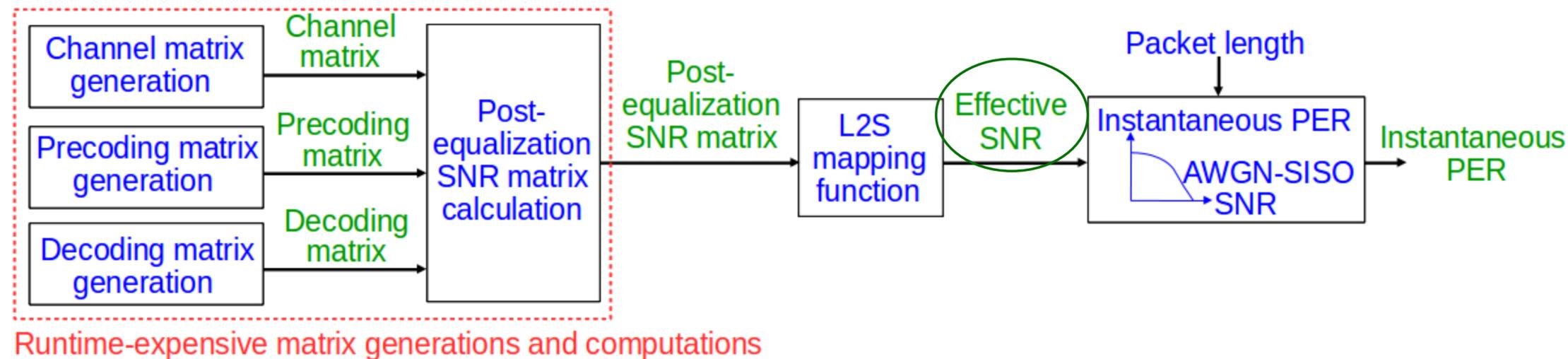
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$$\begin{aligned}
 X &\triangleq \ln(\Gamma_{eff,k}^{sinr}) \\
 &\sim \text{SGN}(\hat{\mu}, \hat{\sigma}, \hat{\lambda}_1, \hat{\lambda}_2)
 \end{aligned}
 \quad
 \begin{aligned}
 &f_X(x; \hat{\mu}, \hat{\sigma}, \hat{\lambda}_1, \hat{\lambda}_2) \quad \text{PDF of } X \\
 &= \frac{2}{\hat{\sigma}} \psi\left(\frac{x - \hat{\mu}}{\hat{\sigma}}\right) \Psi\left(\frac{\hat{\lambda}_1(x - \hat{\mu})}{\sqrt{\hat{\sigma}^2 + \hat{\lambda}_2(x - \hat{\mu})^2}}\right), \quad x \in \mathbf{R},
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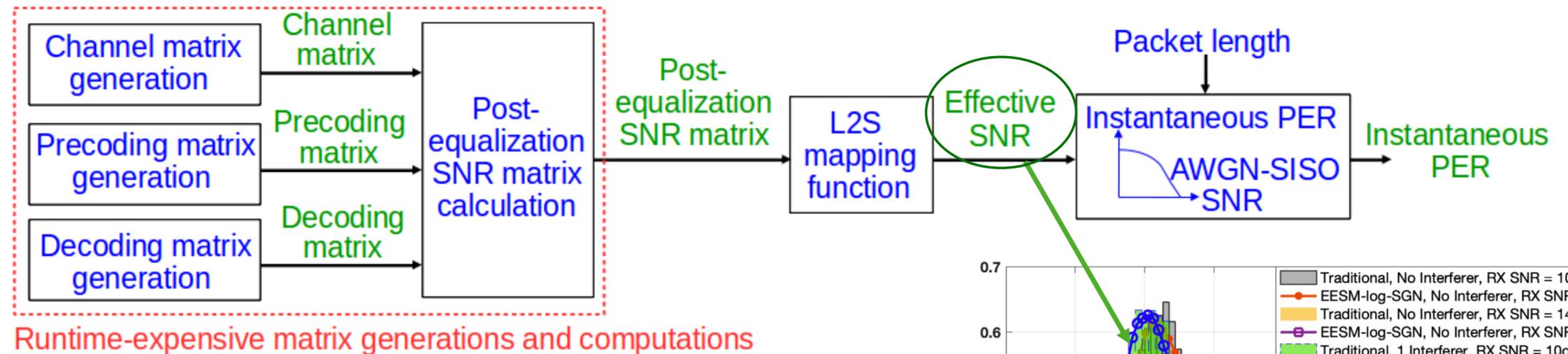
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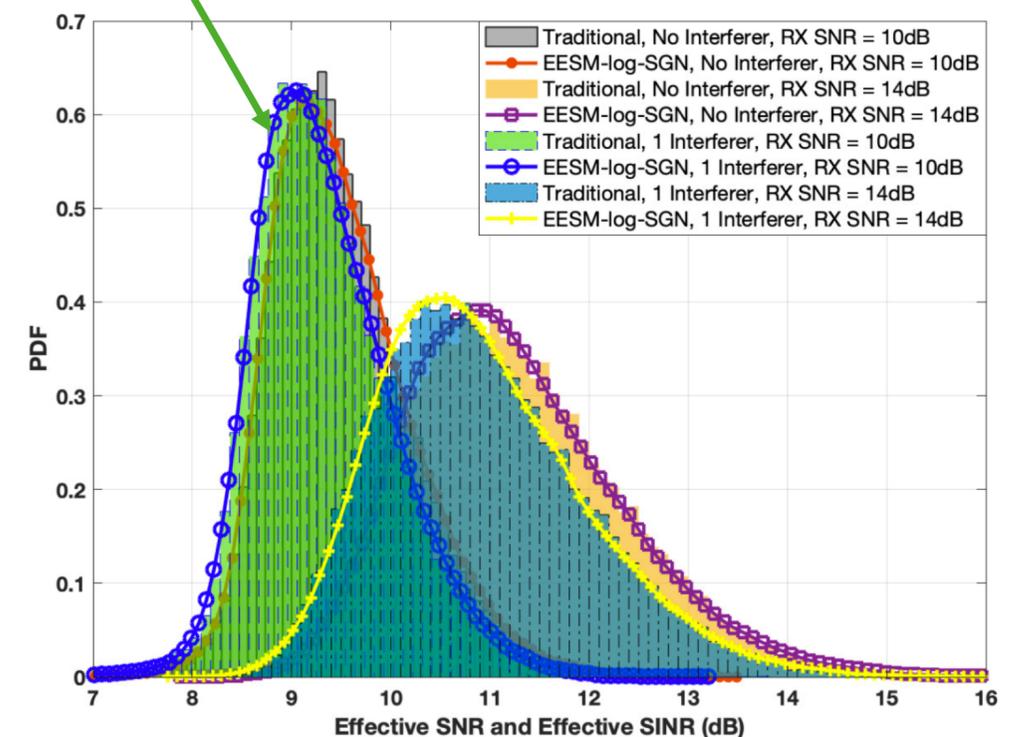
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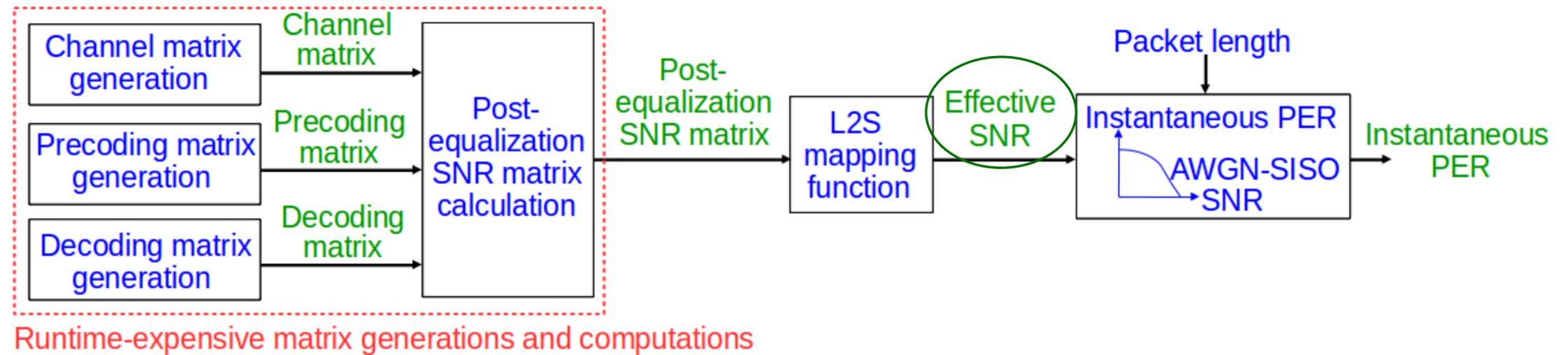
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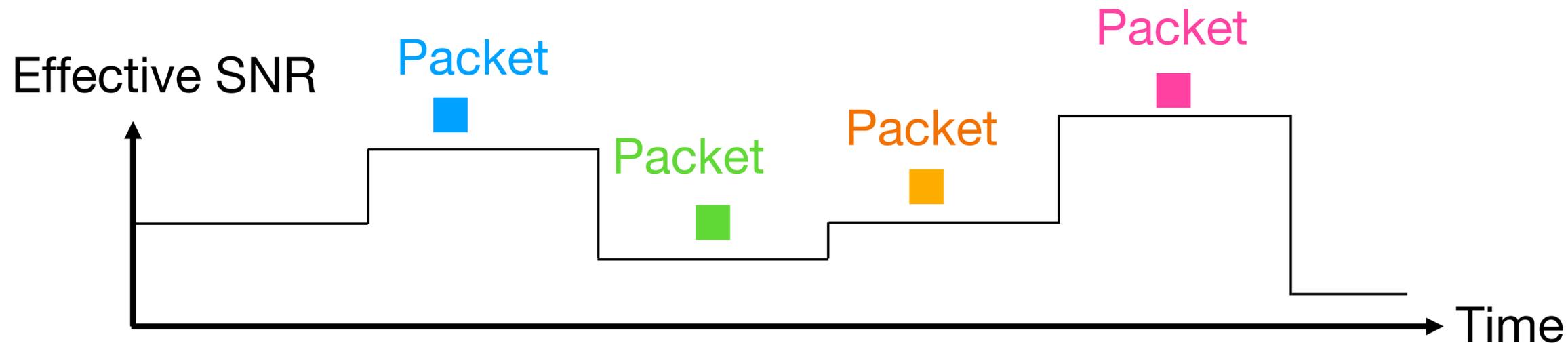
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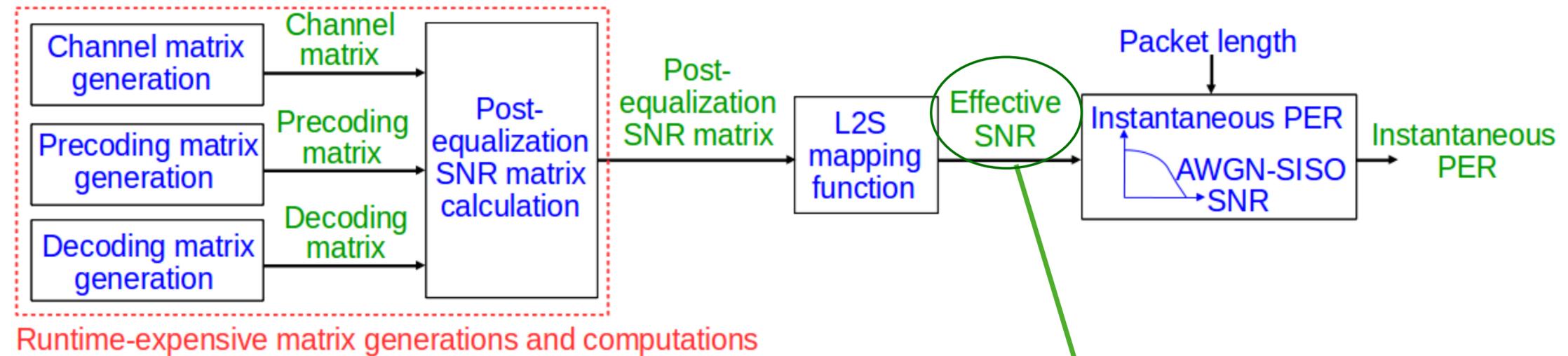


Assume IID channel for different packets



Sub-6GHz Wi-Fi Time-varying Channel

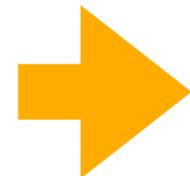
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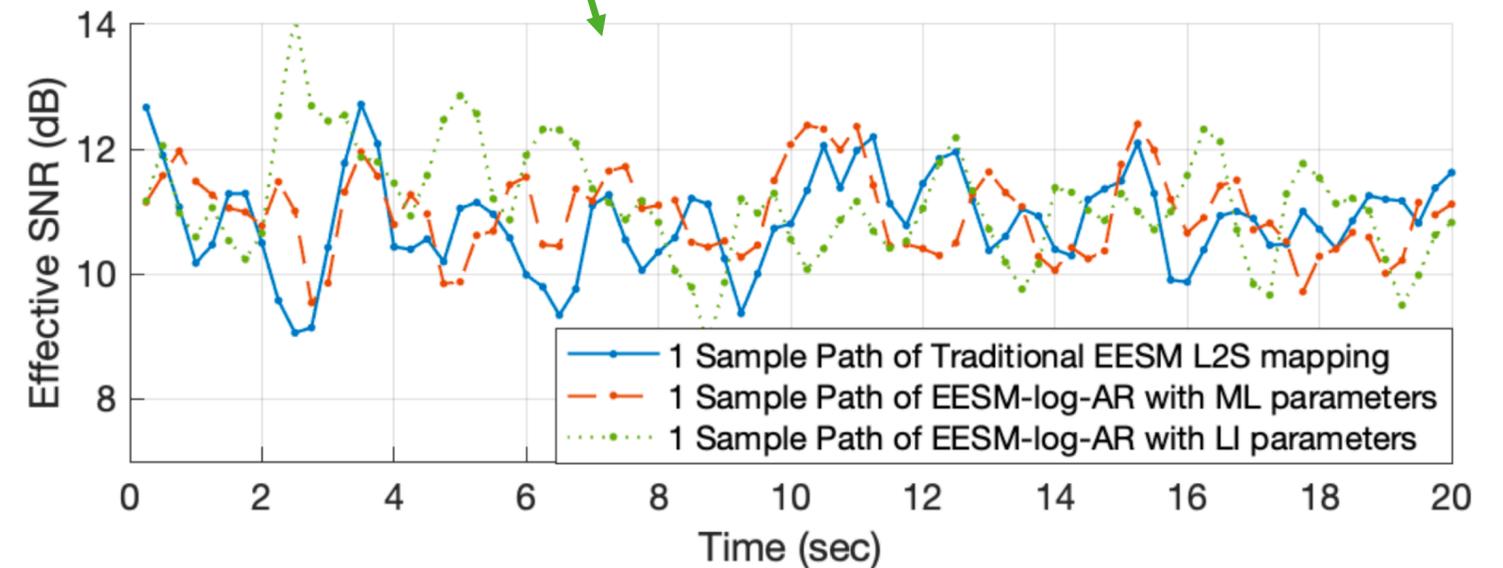
Sub-6GHz Wi-Fi channel is time-varying

Have correlations

Vary slowly overtime

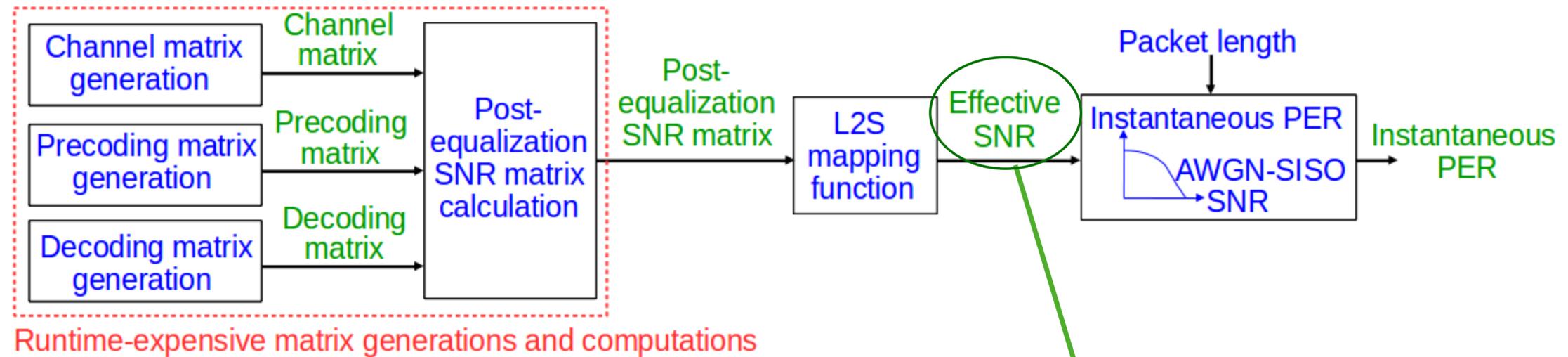


Burst error



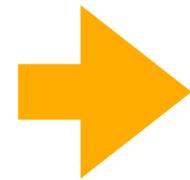
Real Wi-Fi Time-varying Channel

L2S mapping:

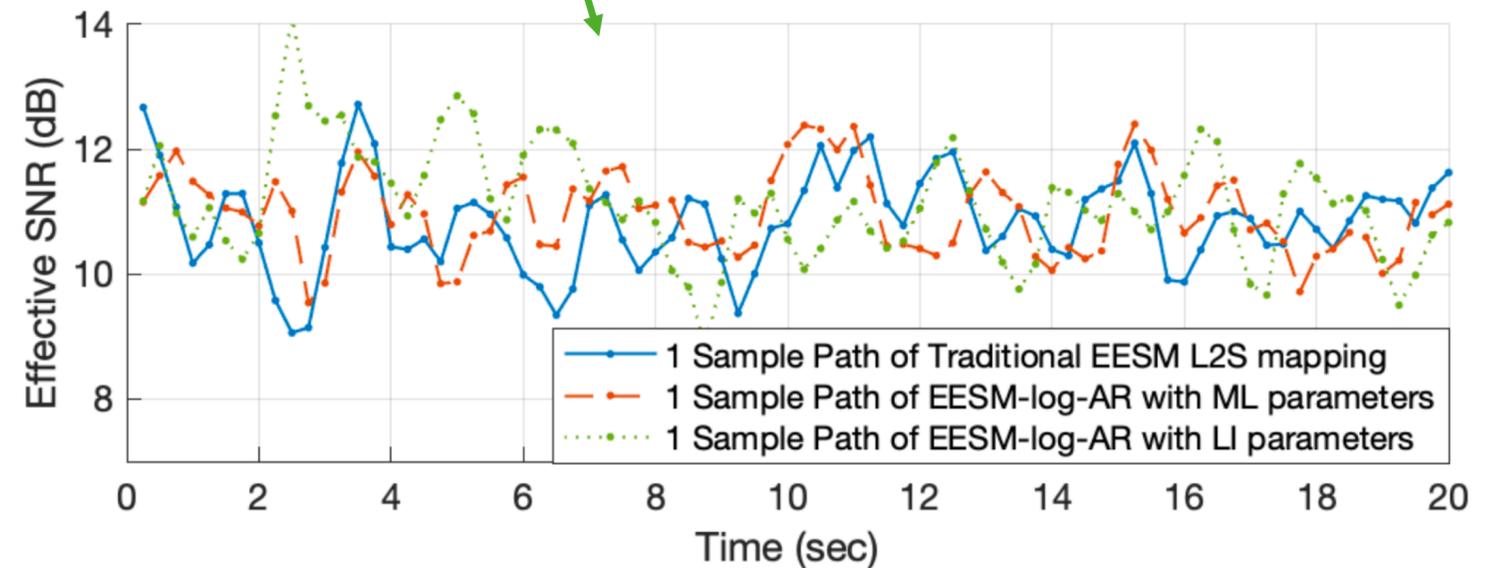


Real Wi-Fi channel: time-varying channel

Have correlations
Vary slowly overtime



Burst error

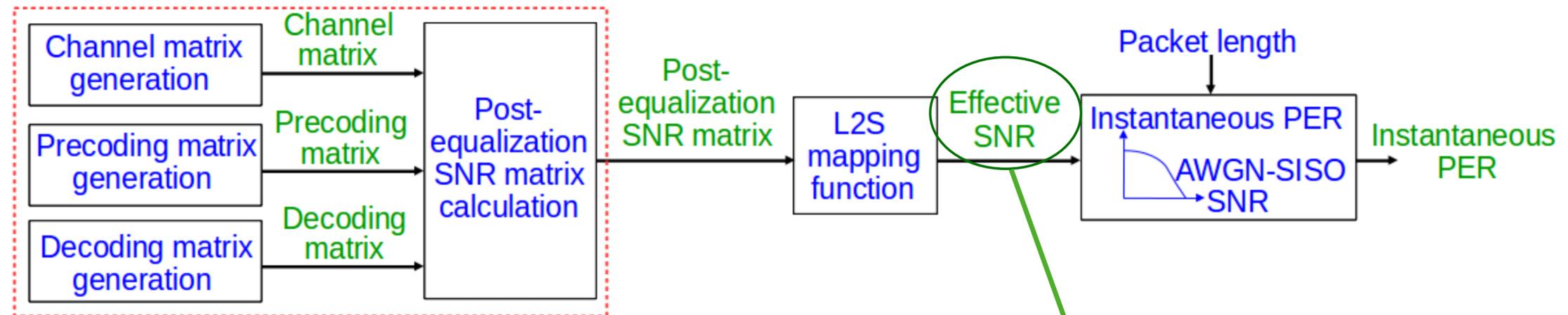


Extend EESM-log-SGN method to time-varying channel



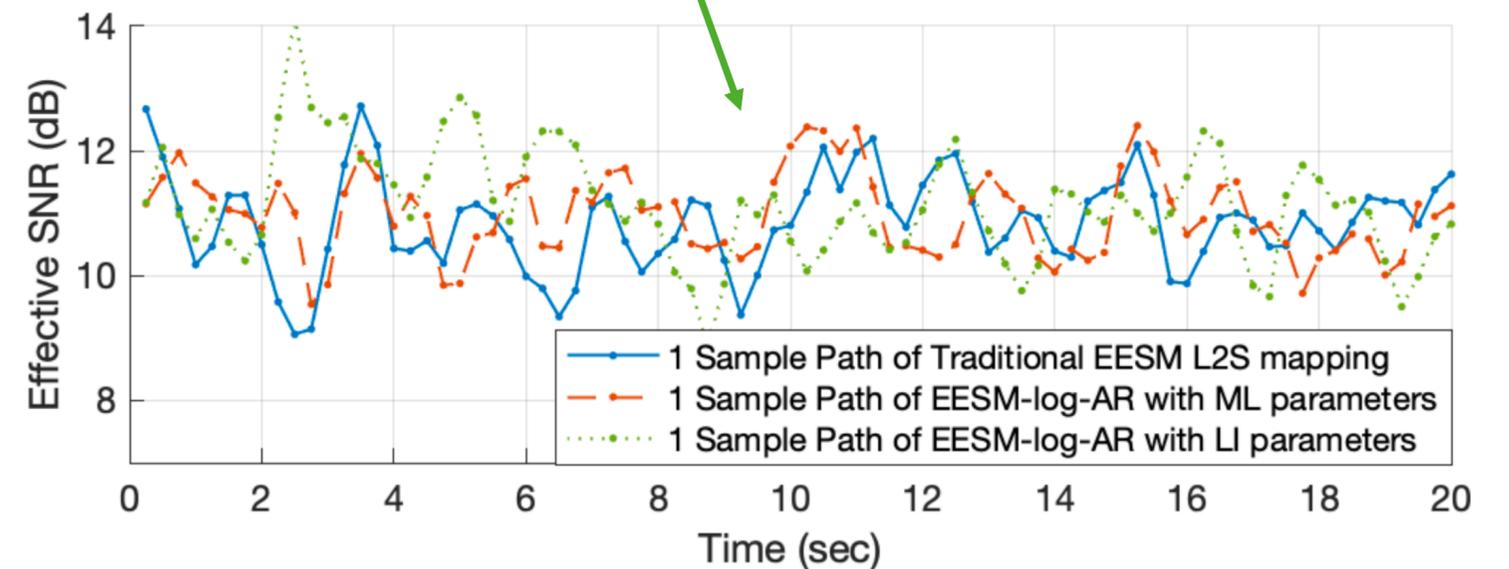
EESM-log-AR: Main Idea

L2S mapping:



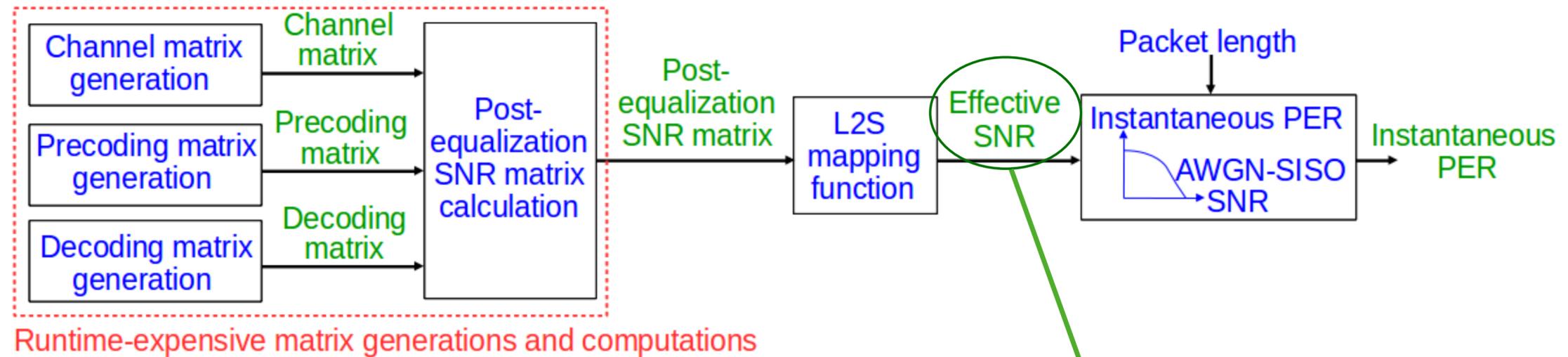
Runtime-expensive matrix generations and computations

Assume **time-varying channel**, model **effective SNR process**, and **directly outputs** effective SNR process



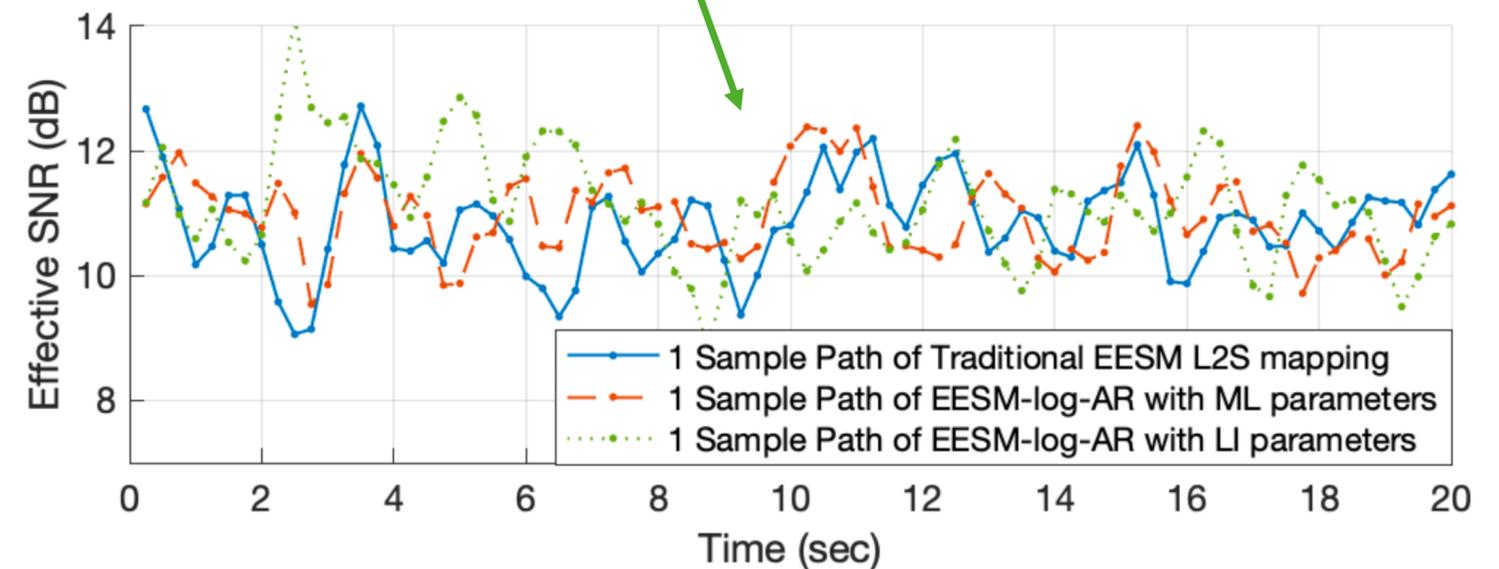
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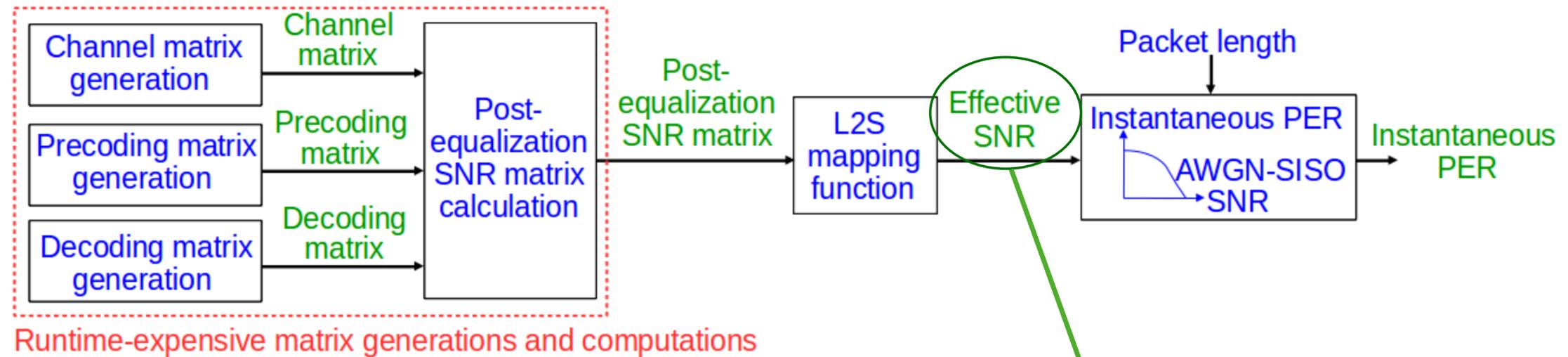
Under time-varying channel & EESM L2S mapping function, effective SNR process follows:

Log-AutoRegressive (log-AR) process



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L2S mapping:



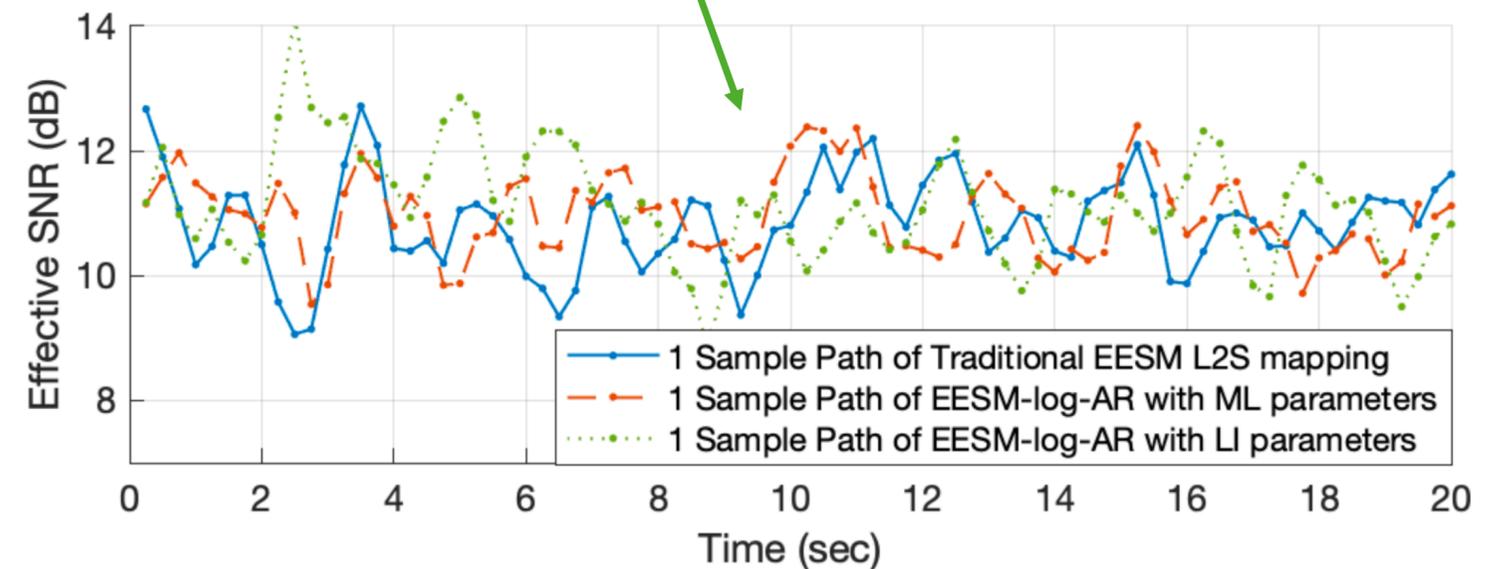
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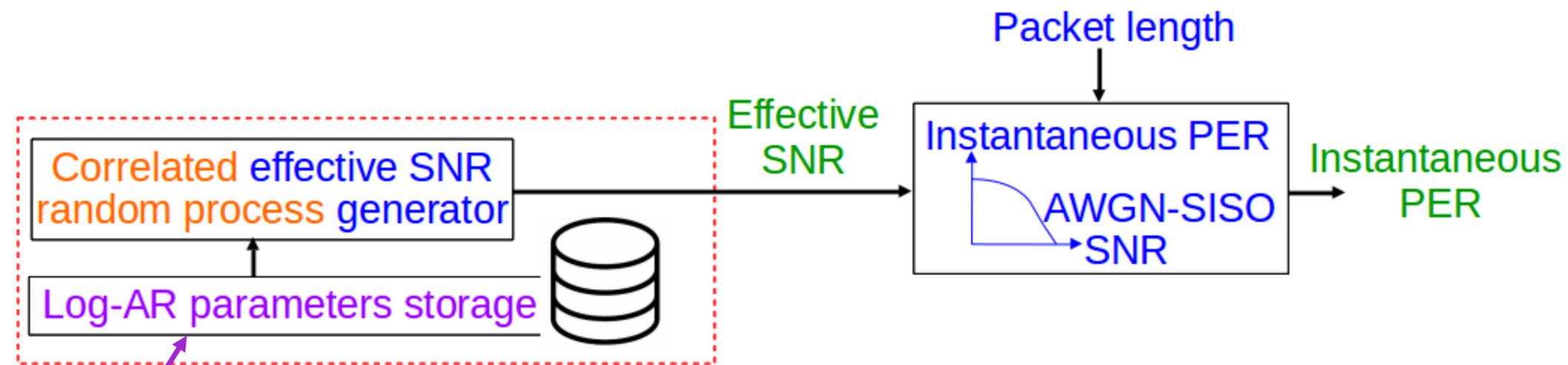
$X[l] \triangleq \ln(\Gamma_{eff}[l])$ Take log of effective SNR

$$X[l] = c + \sum_{m=1}^p \phi_m X[l-m] + \epsilon[l] \quad \text{AR model}$$

Normal variable



EESM-log-AR: Main Idea

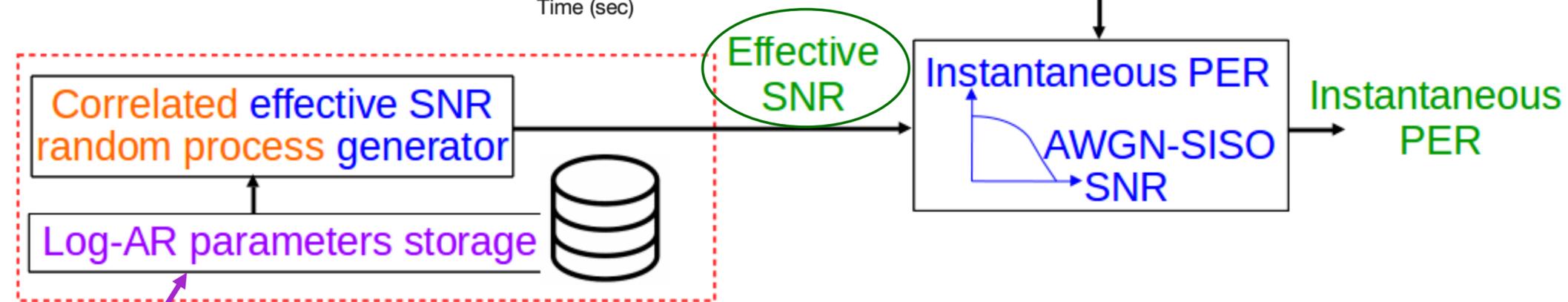
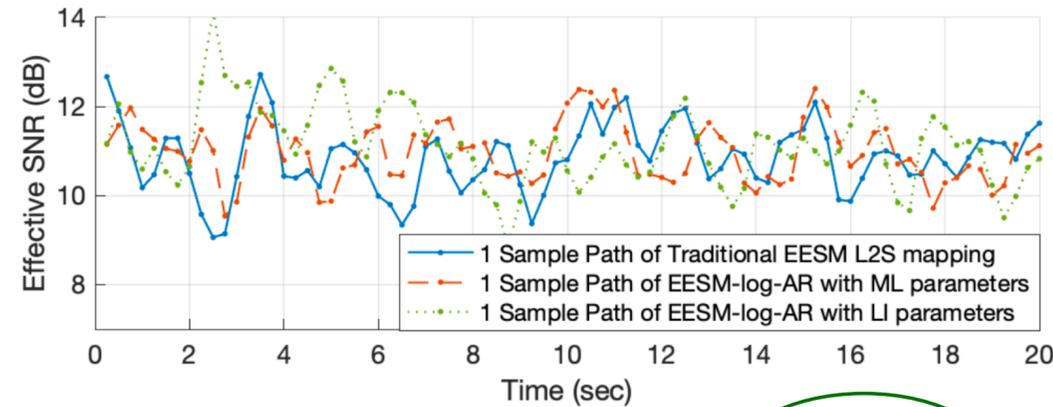


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EESM-log-AR: Main Idea

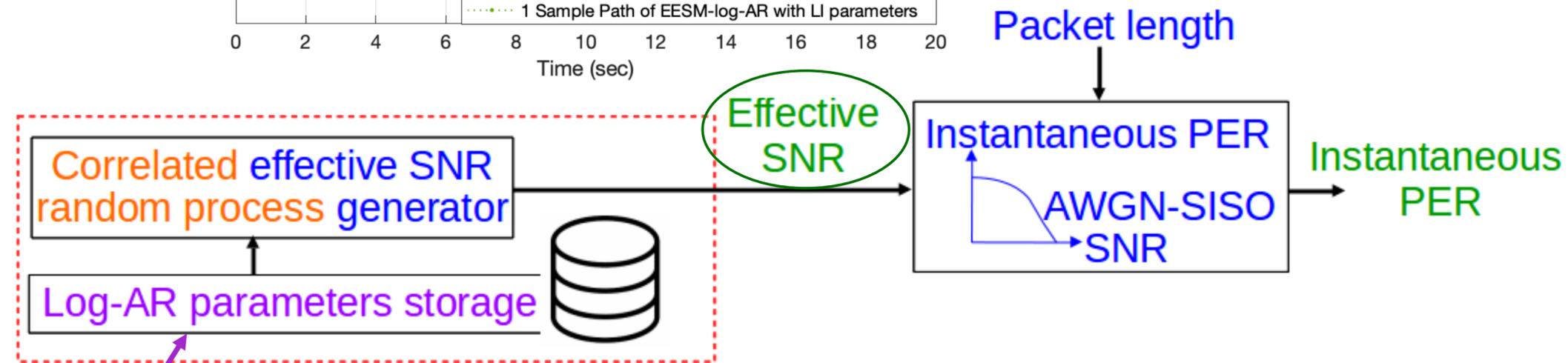
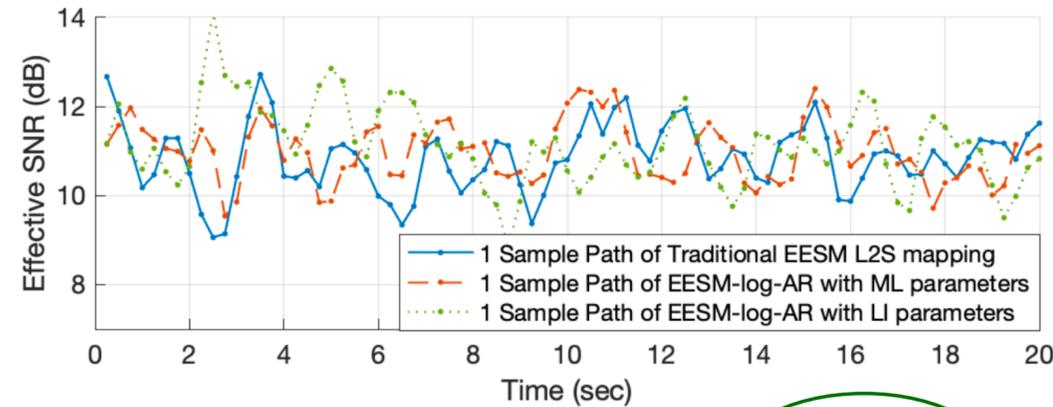


Log-AutoRegressive (log-AR) process

$X[l] \triangleq \ln(\Gamma_{eff}[l])$ Take log of effective SNR

$$X[l] = \underbrace{c} + \sum_{m=1}^p \underbrace{\phi_m X[l-m]} + \epsilon[l] \quad \text{AR model}$$

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log-AR parameters depend on:
MIMO setup, bandwidth, MCS,
and channel types

EESM-log-AR: Runtime

Runtime of single link 200,000-packet simulation (Table 4)

$N_t \times N_r$	Bandwidth	L2S Mapping	EESM-log-AR
1×1	20MHz	97 min	0.4 sec
1×1	40MHz	126 min	0.4 sec
4×2	20MHz	234 min	0.4 sec
4×2	40MHz	320 min	0.4 sec
8×2	20MHz	428 min	0.4 sec
8×2	40MHz	573 min	0.4 sec

Runtime of the proposed method is significantly smaller and insensitive to system dimension change

EESM-log-AR: Accuracy

EESM-log-AR: Accuracy

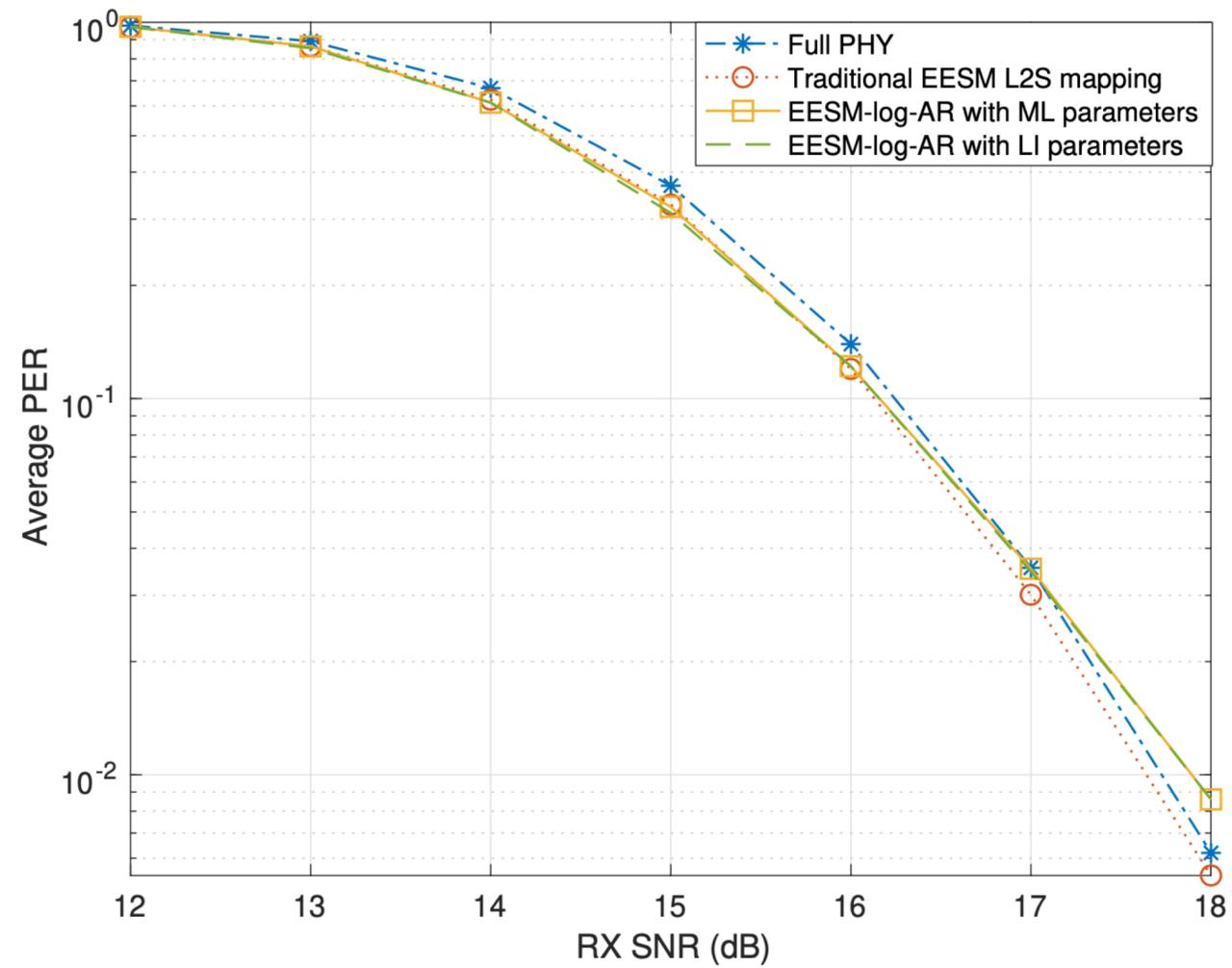
1st order performance: Average PER VS. RX SNR

EESM-log-AR: Accuracy

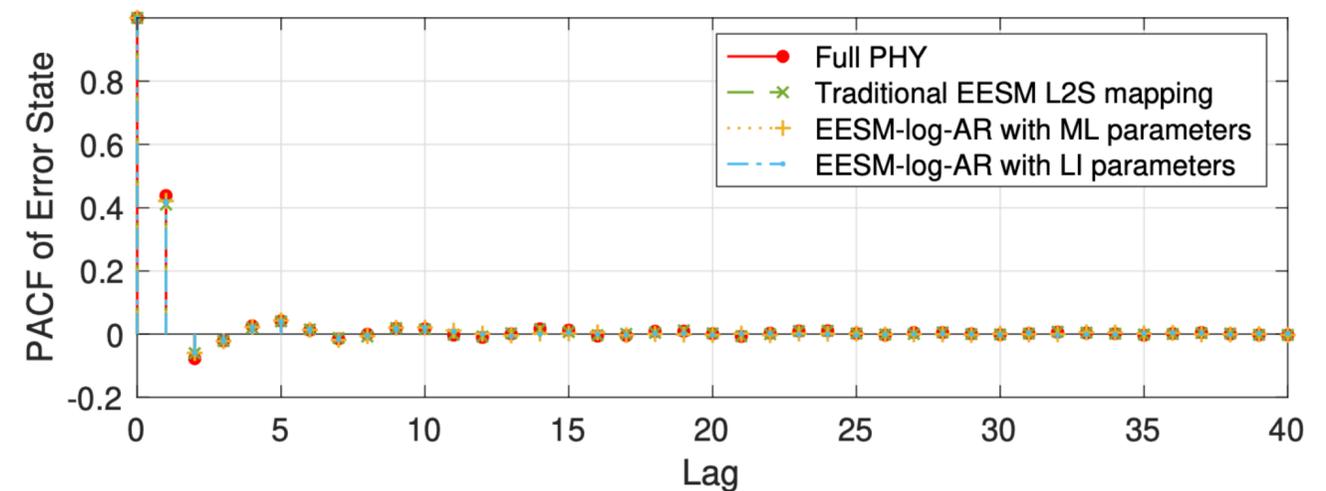
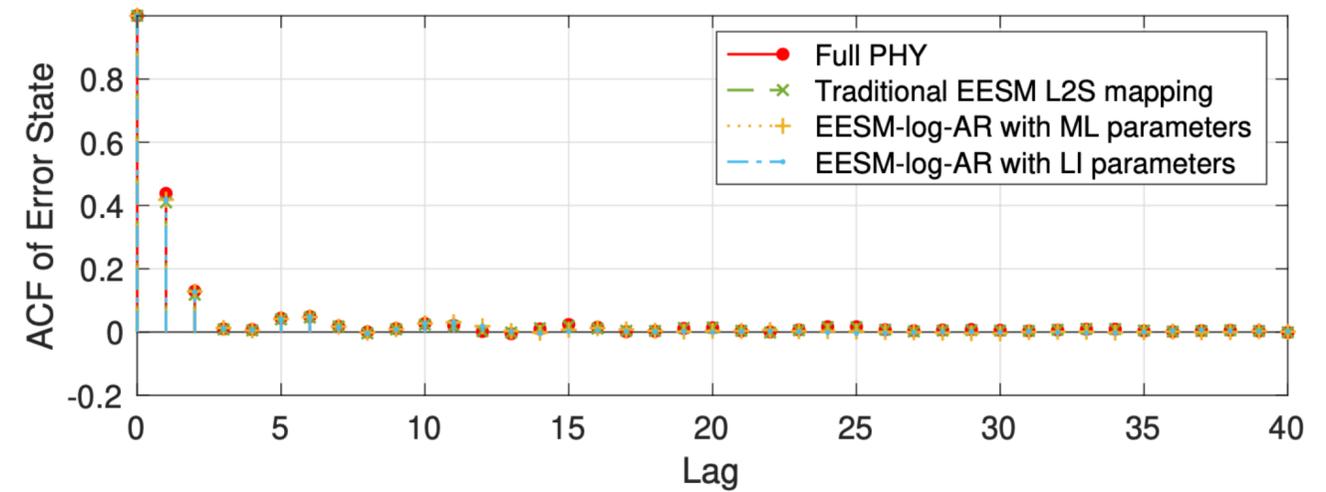
1st order performance: Average PER VS. RX SNR

2nd order performance: AutoCorrelation Function (ACF) and Partial ACF (PACF)

EESM-log-AR: Accuracy

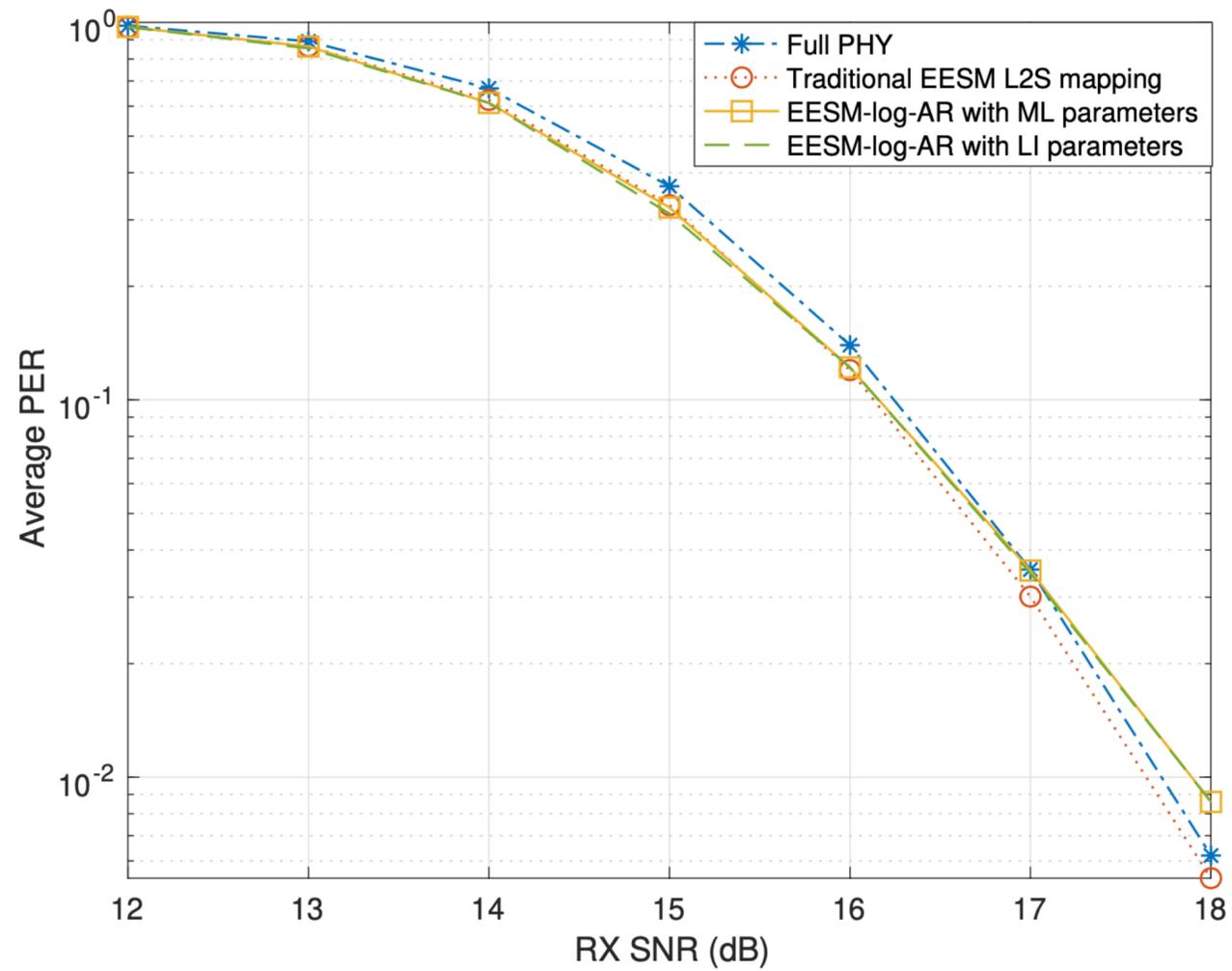


1st order performance: Average PER VS. RX SNR

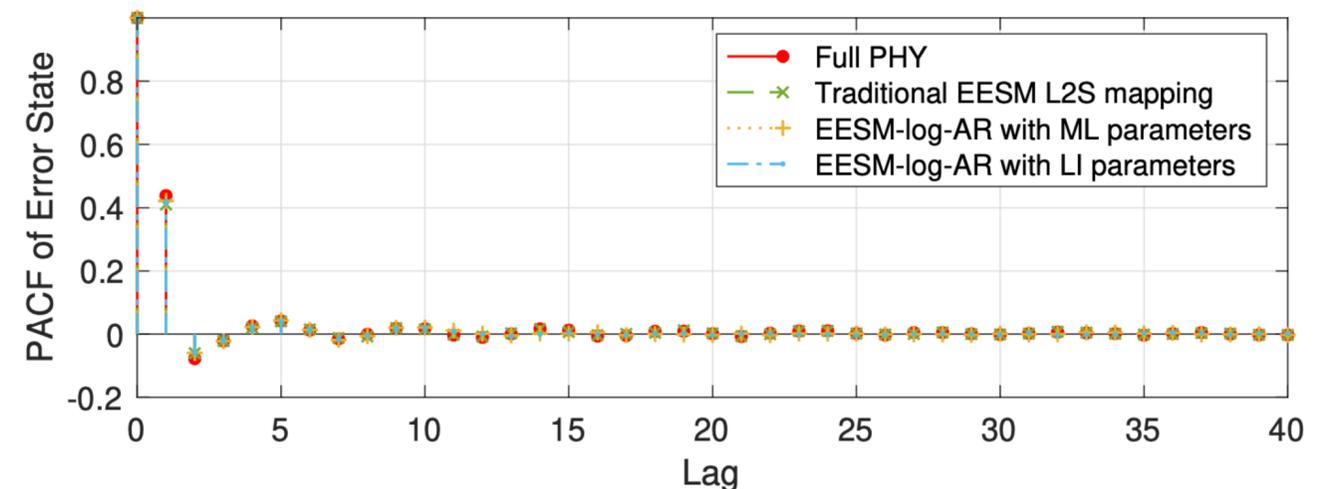
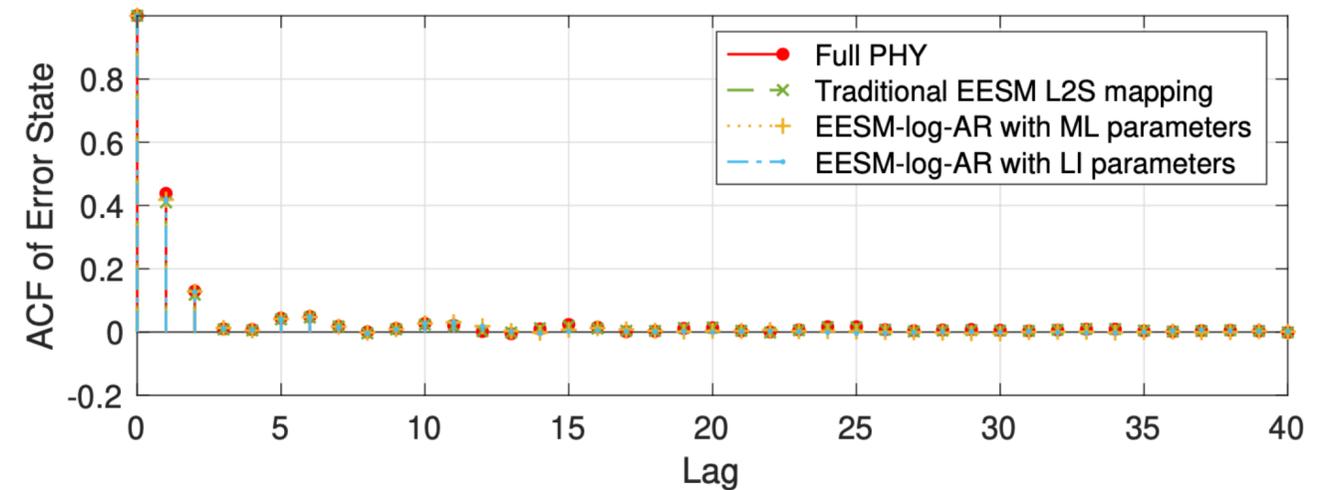


2nd order performance: AutoCorrelation Function (ACF) and Partial ACF (PACF)

EESM-log-AR: Accuracy



1st order performance: Average PER VS. RX SNR



2nd order performance: AutoCorrelation Function (ACF) and Partial ACF (PACF)

We also **validated** EESM-log-AR using **modified LMC test & residual diagnoses**

Contributions

- Under **time-varying channel**, EESM-log-AR directly outputs **effective SNR process** rather than generating channels and calculating effective SNR on a per-packet basis

Contributions

- Under **time-varying channel**, EESM-log-AR directly outputs **effective SNR process** rather than generating channels and calculating effective SNR on a per-packet basis
- Payoff: **good accuracy with substantial run-time improvements**
- Cost: require store log-AR parameters at different PHY configurations

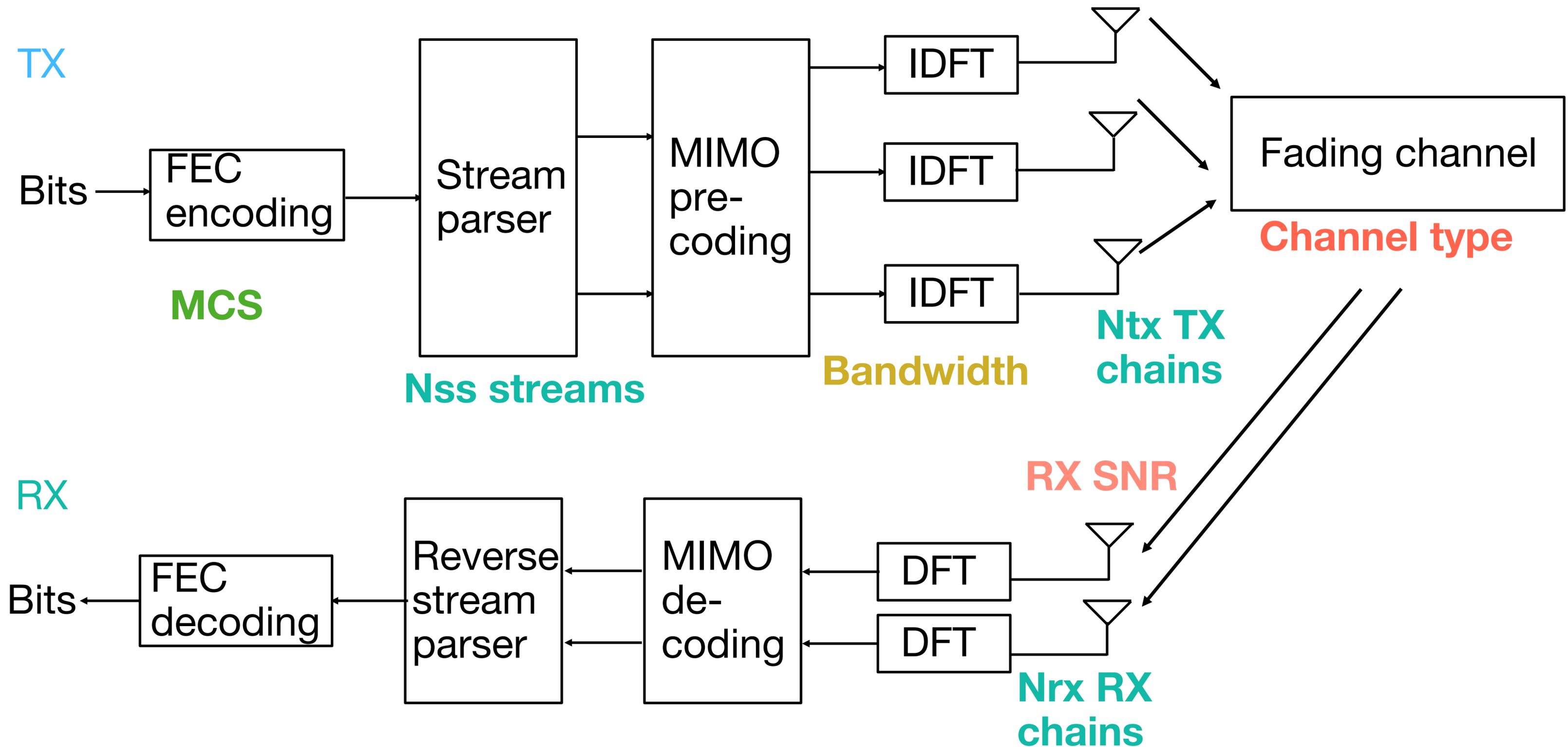
Contributions and Future Work

- Under **time-varying channel**, EESM-log-AR directly outputs **effective SNR process** rather than generating channels and calculating effective SNR on a per-packet basis
- Payoff: **good accuracy with substantial run-time improvements**
- Cost: require to store log-AR parameters at different PHY configurations
- Future work:
 - Model the impact of interference
 - Extension to OFDMA and MU-MIMO cases

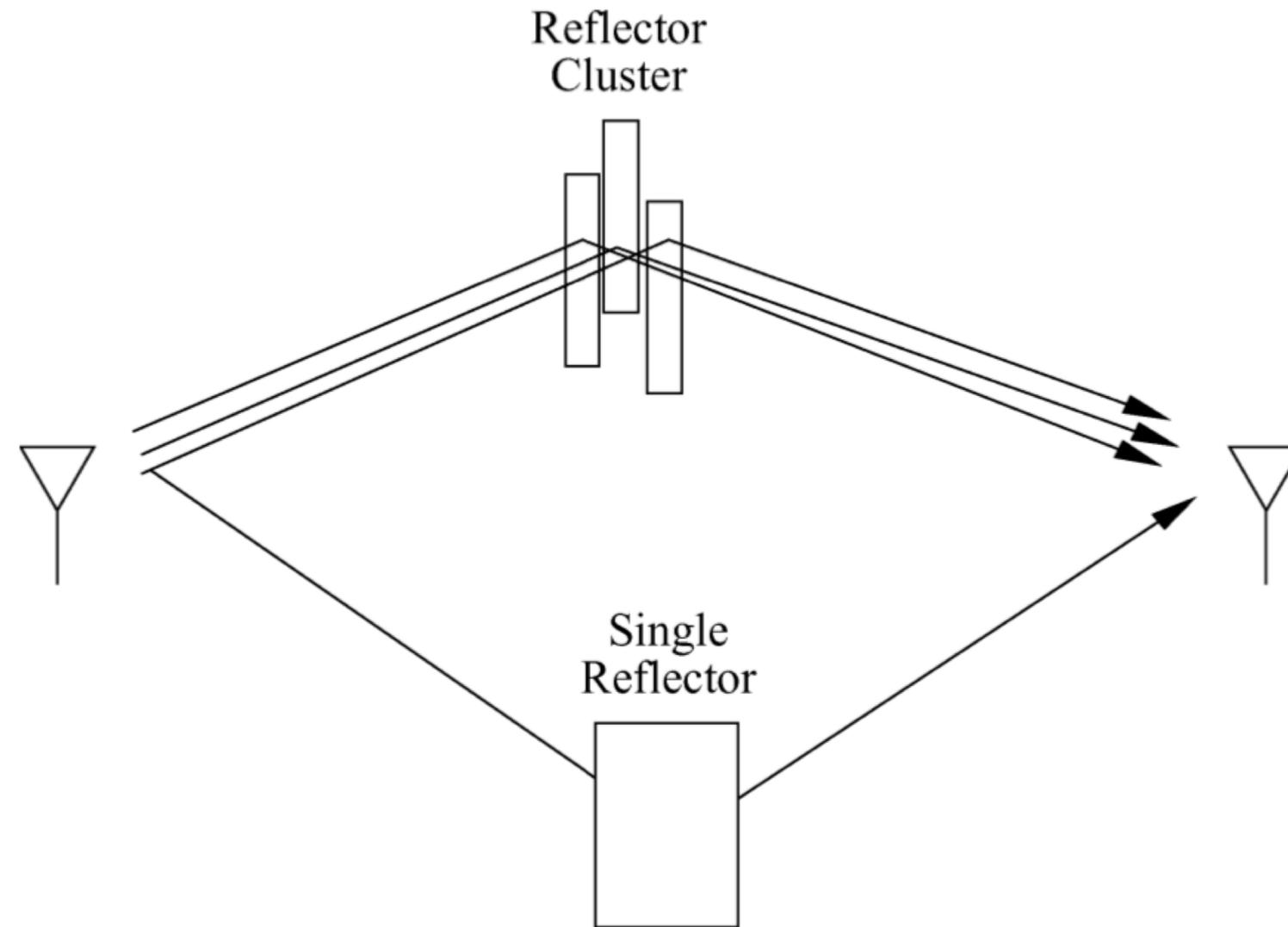
Backup Slides



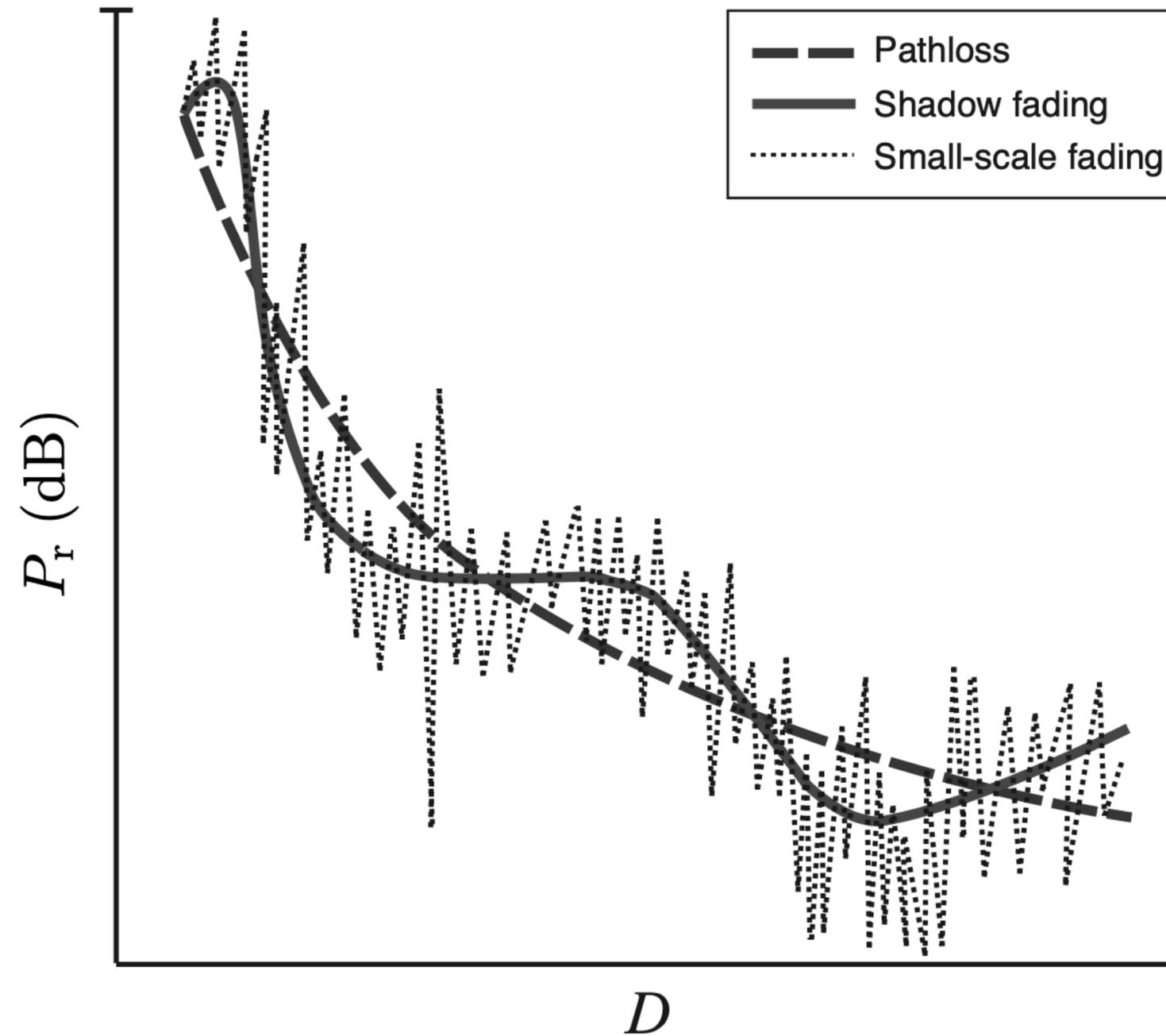
Full-PHY Block Diagram



Multi-path Propagation



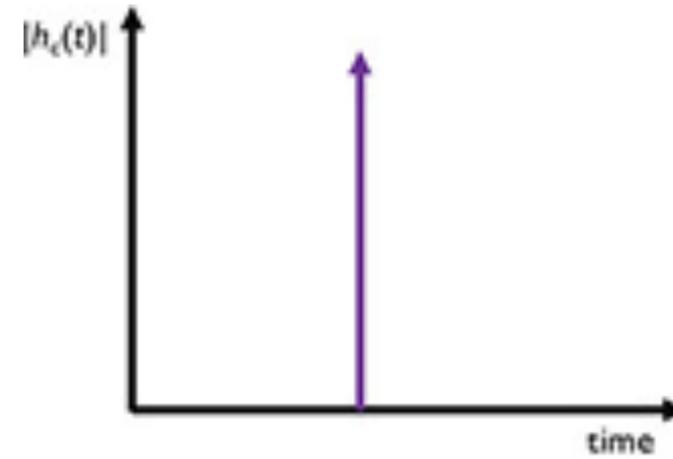
Fading



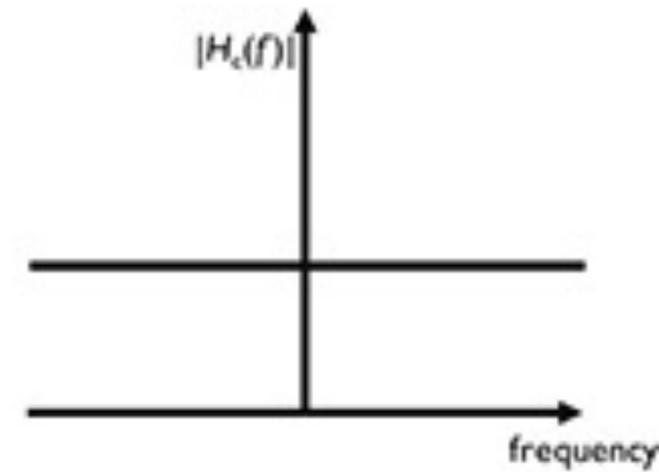
Received signal power VS. distance

Frequency-selective Channel

LOS

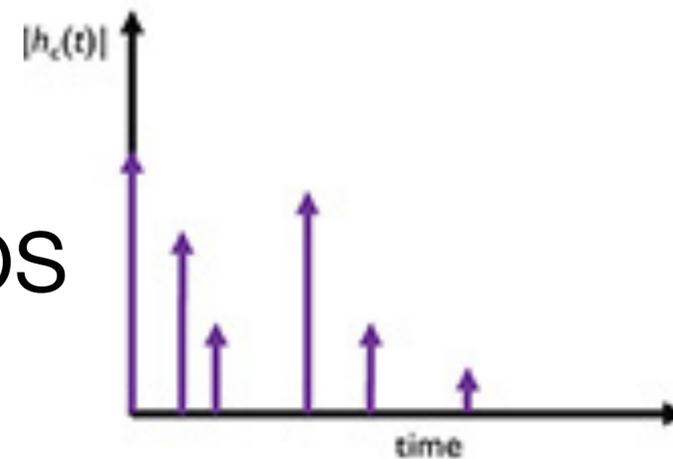


(a)

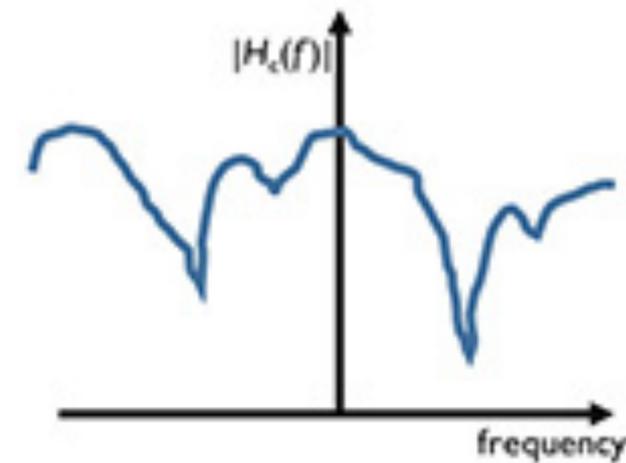


Frequency flat

LOS +
multi-path NLOS

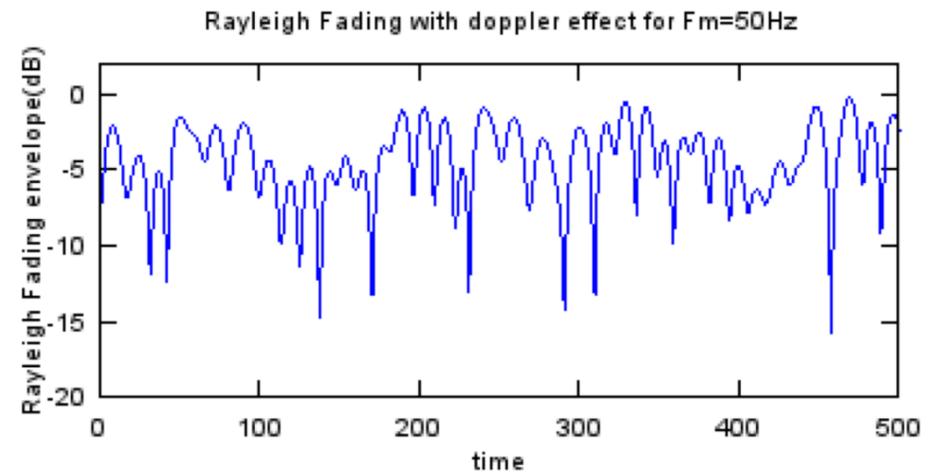
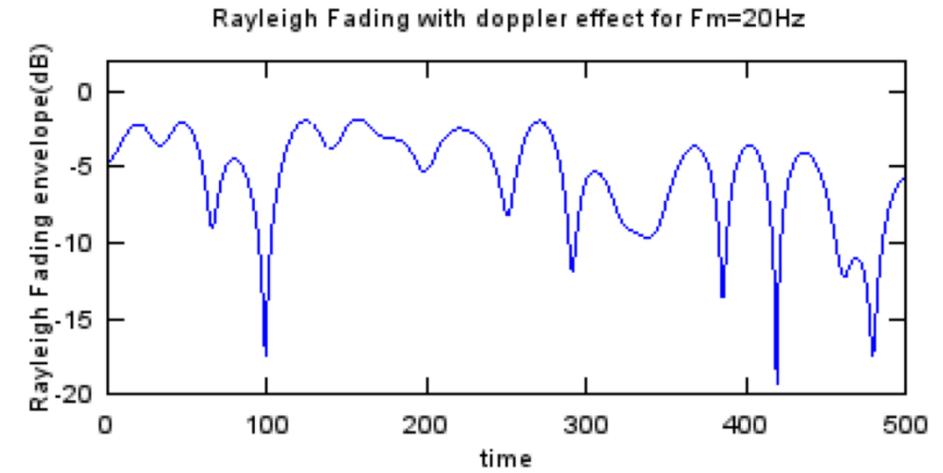
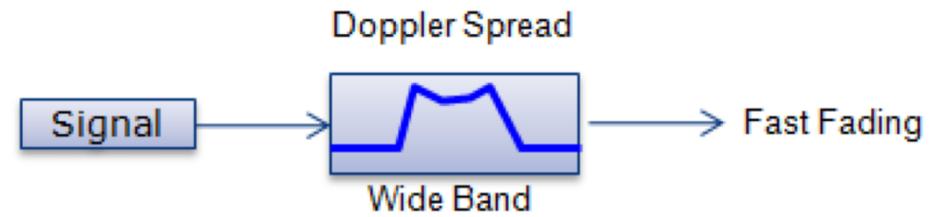
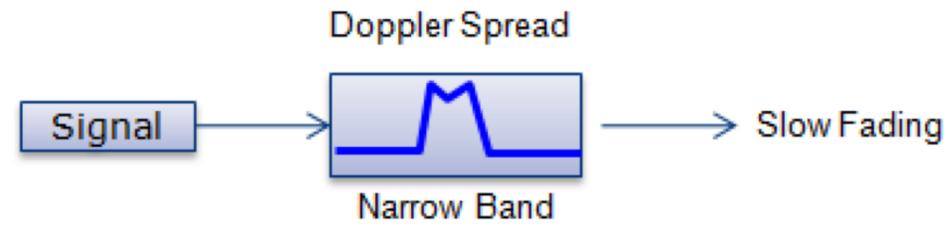
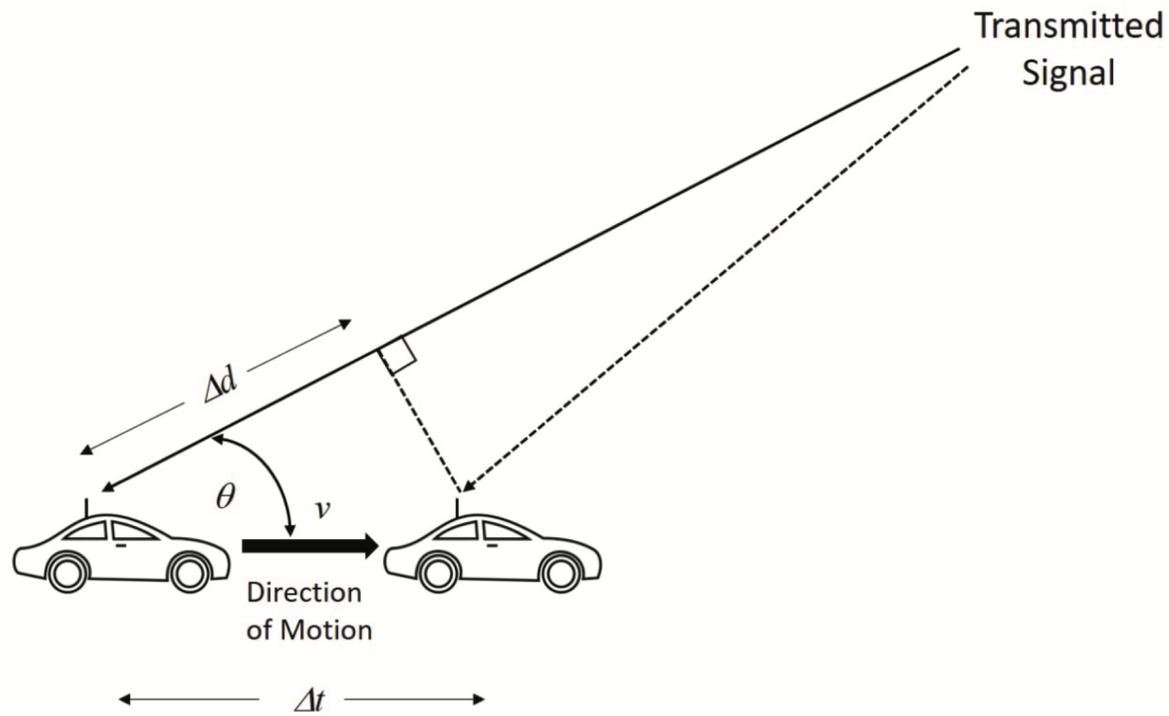


(b)



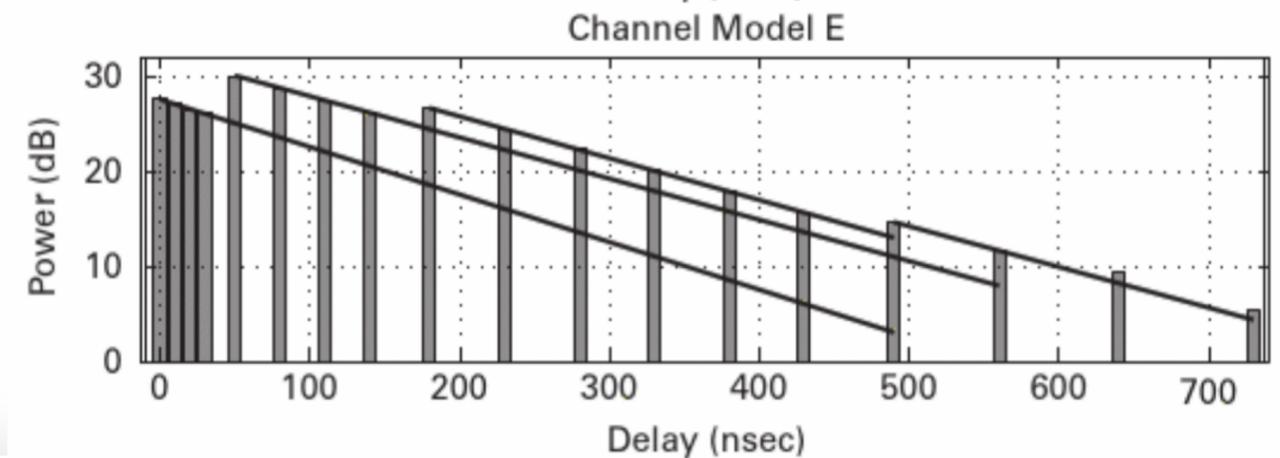
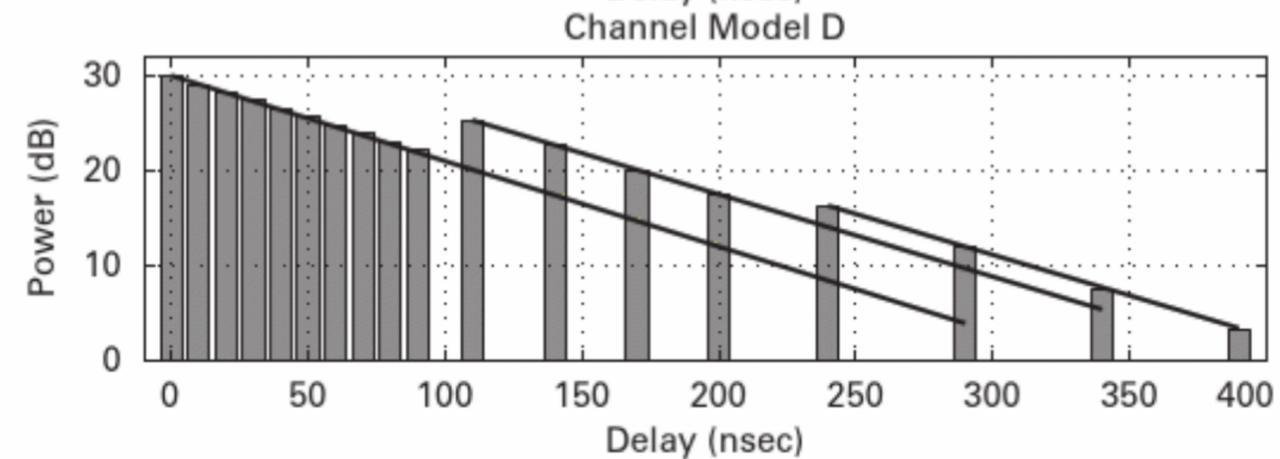
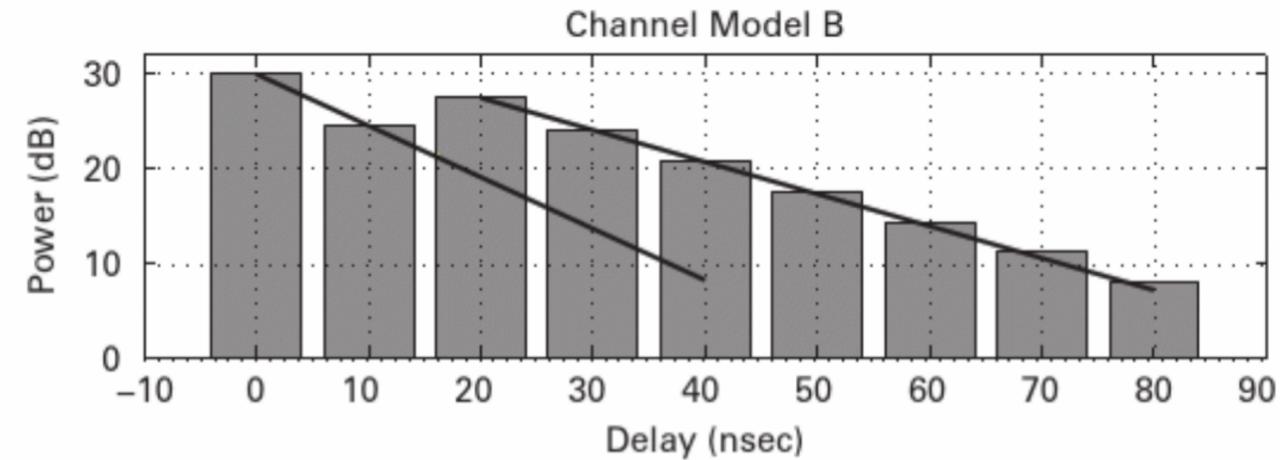
Frequency selective

Time-varying Channel

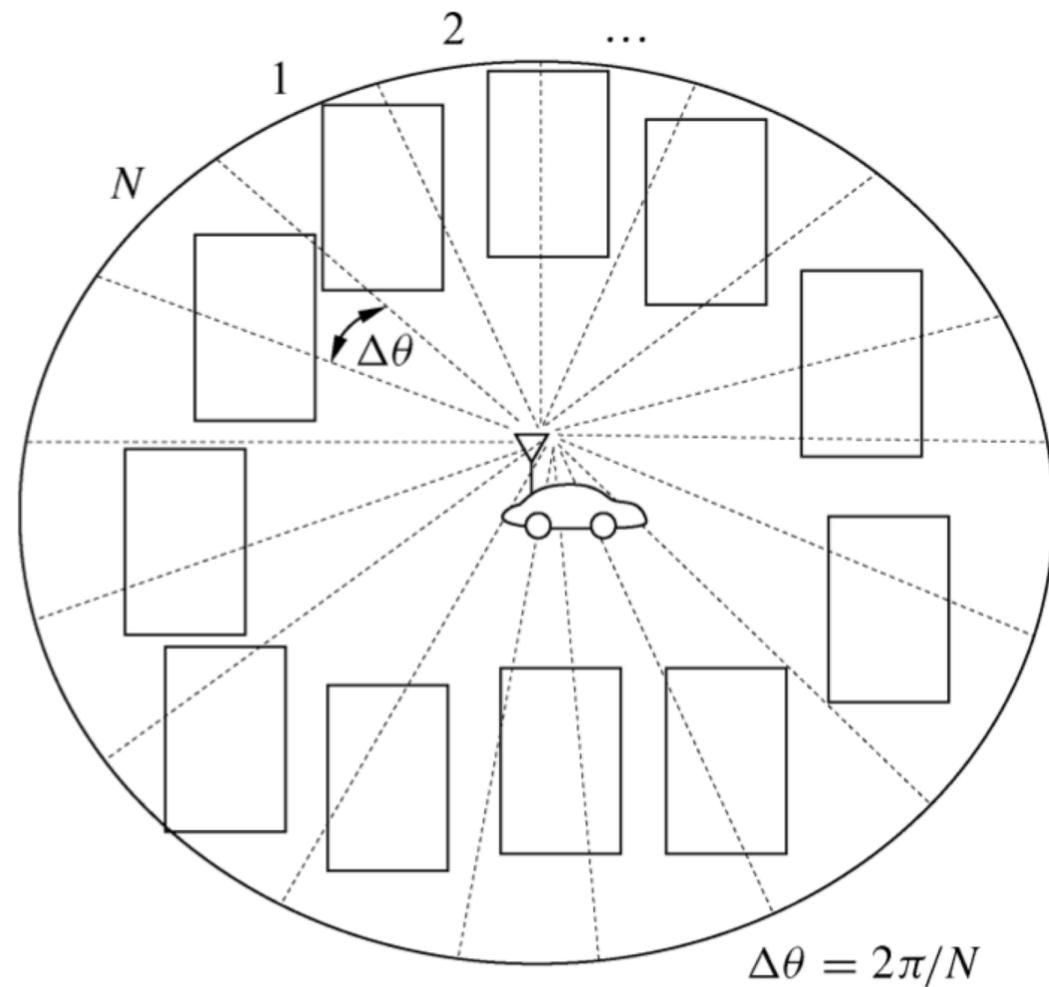


TGax Channel Models

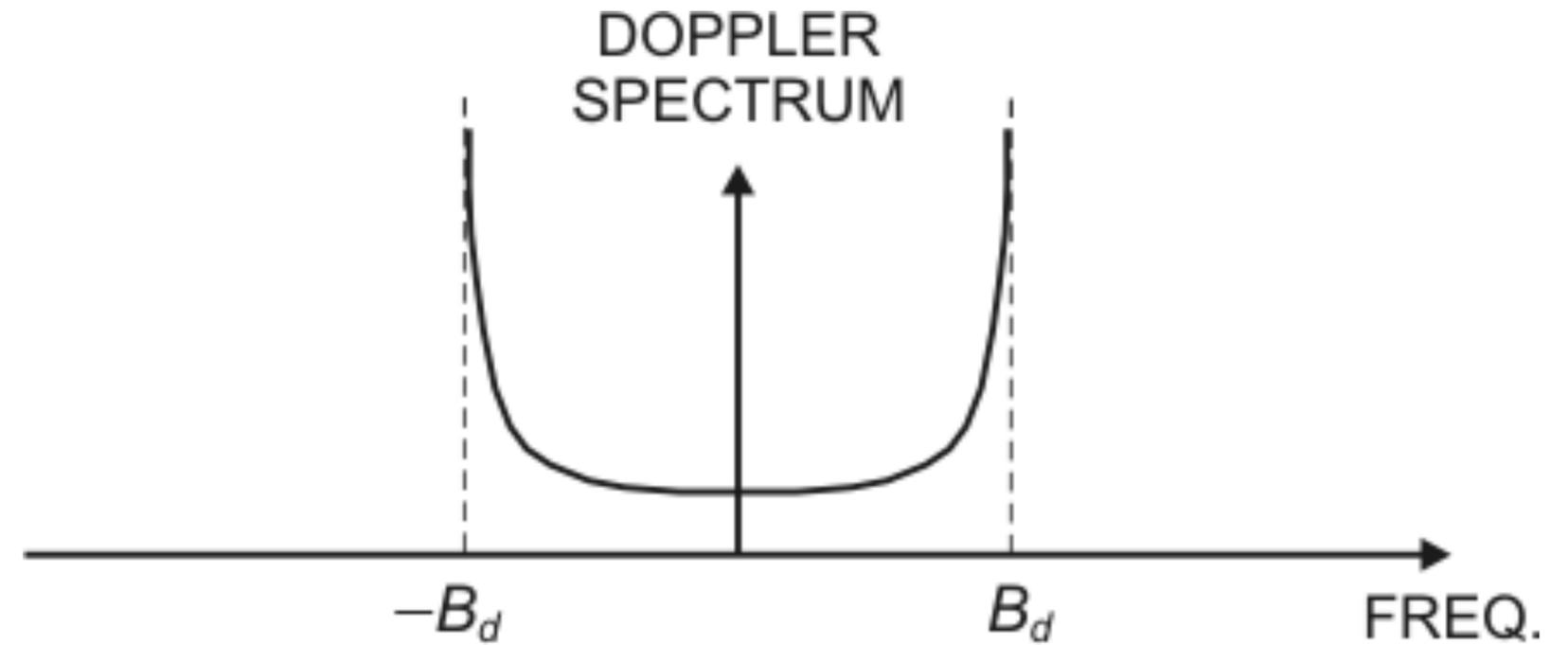
TGax channel
Models: A~F



Jakes' Model



Uniform scattering environment



Doppler spectrum

PHY Layer Simulation Setup

Communication system	IEEE 802.11ax
Link simulator	MATLAB WLAN & Communication Toolboxes R2020b
# of packets per simulation	200000
Channel type	TGax channel model-D [22]
Doppler spectrum	Jakes' model [1]
Maximum moving speed	0.089km/h [29]
Coherence time	$T_c = 0.978s$ [32]
Sample period	$T_s = 0.250s$
Channel coding	LDPC
Payload length	1000
MCS	4
RX SNR	15dB
Bandwidth	20 MHz
Channel estimation	Noise-free
Phase tracking & Synchronization	Perfect
MIMO precoding/decoding	SVD/MMSE
MIMO dimension	$n_t \times n_r = 4 \times 2$
MIMO streams	$n_{ss} = 2$
CPU	Intel Core i5 CPU at 2.0GHz

Properties of log-AR process

Properties of log-AR process:

- 1) fully characterized by $p+2$ parameters;
- 2) easy to generate;
- 3) but cannot capture skewness and kurtosis of marginal distribution well.

$$X[l] \triangleq \ln(\Gamma_{eff}[l])$$

$$X[l] = c + \sum_{m=1}^p \phi_m X[l-m] + \epsilon[l]$$

Traditional L2S Mapping

- Over an OFDM/OFDMA MIMO/MU-MIMO system, abstracting the post-MIMO processing SINRs over all subcarriers and spatial streams into a *single* scalar metric - **effective SNR**

$$\Gamma_{eff,k}^{sinr} = \alpha \Phi^{-1} \left(\frac{1}{n_{sc,k}} \frac{1}{n_{ss,k}} \sum_{i \in \mathcal{N}_{sc,k}} \sum_{j=1}^{n_{ss,k}} \Phi \left(\frac{\Gamma_{k,i,j}}{\beta} \right) \right)$$

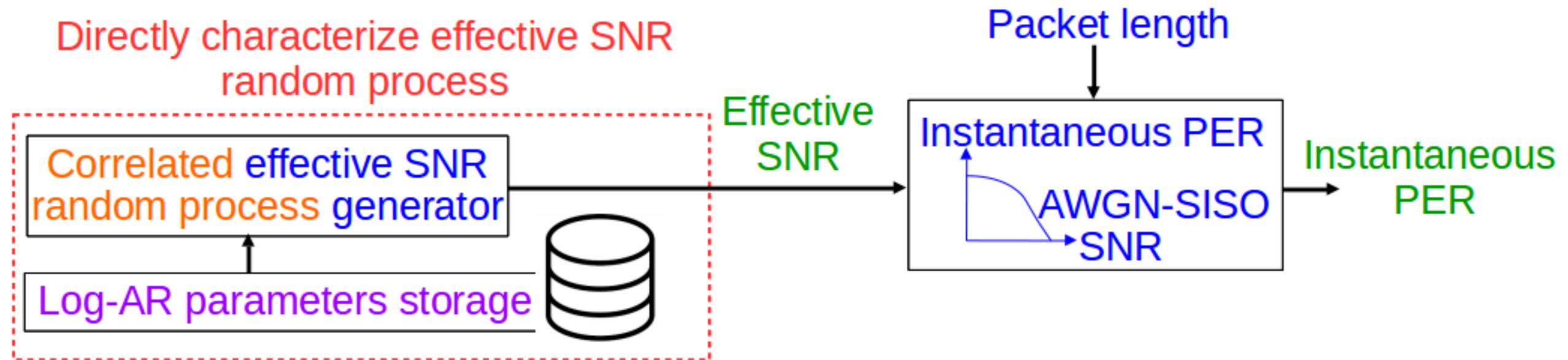
L2S mapping function

- The single effective SINR is a convenient metric to describe the packet-level performance for a network simulator
- 2 popular L2S mapping functions: EESM and RBIR

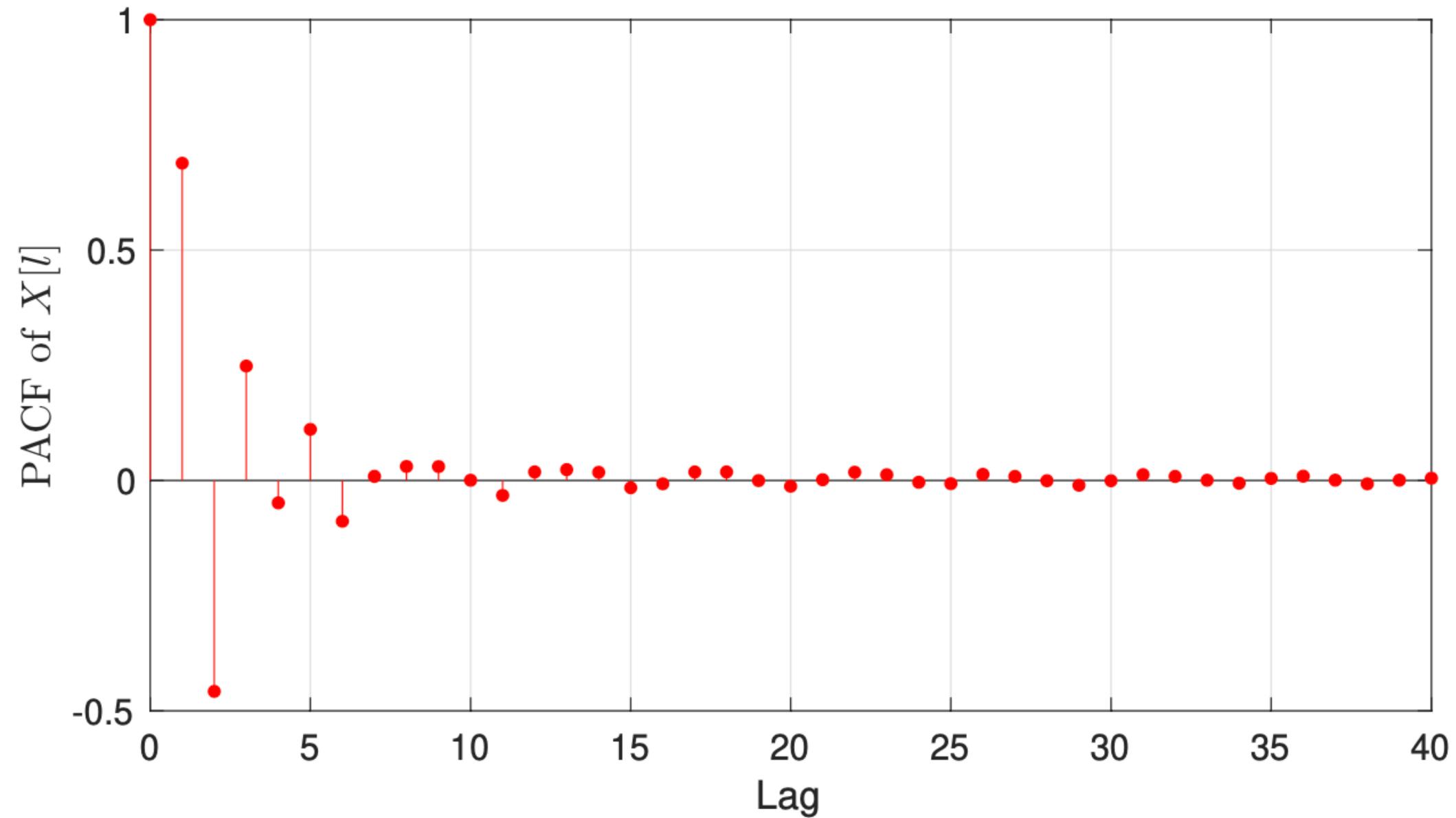
- For EESM, $\Phi(x) = \exp(-x)$ and $\alpha = \beta$

$$\Gamma_{eff,k}^{sinr} = -\beta \ln \left(\frac{1}{n_{sc,k}} \frac{1}{n_{ss,k}} \sum_{i \in \mathcal{N}_{sc,k}} \sum_{j=1}^{n_{ss,k}} \exp \left(-\frac{\Gamma_{k,i,j}}{\beta} \right) \right)$$

EESM-log-SGN



PACF of Effective SNR Processes



ML Estimation of Log-AR Parameters

RX SNR γ	$\hat{c}(\gamma)$	$\hat{\phi}_1(\gamma)$	$\hat{\phi}_5(\gamma)$	$\hat{\phi}_9(\gamma)$	$\hat{\sigma}_{10}^2(\gamma)$
12dB	0.5764	1.3454	0.3685	0.0607	0.0076
13dB	0.6525	1.2702	0.3068	0.0474	0.0085
14dB	0.7297	1.2047	0.2561	0.0370	0.0096
15dB	0.8093	1.1443	0.2128	0.0294	0.0112

Storage-complexity aspect

Handling wide range of RX SNRs: challenge & principle

- Fact: effective SNR depends on RX SNR
- Challenge: **cannot** store effective SNR process under **any** RX SNR
- Solution: **estimate** effective SNR process for any RX SNR using a small # of stored effective SNR processes - **Linear Interpolated (LI) log-AR parameter estimation**

$$\hat{c}(\gamma) = (1 - \epsilon)\hat{c}(\gamma_1) + \epsilon\hat{c}(\gamma_2),$$

$$\hat{\phi}_m(\gamma) = (1 - \epsilon)\hat{\phi}_m(\gamma_1) + \epsilon\hat{\phi}_m(\gamma_2), \quad m = 1, 2, \dots, p,$$

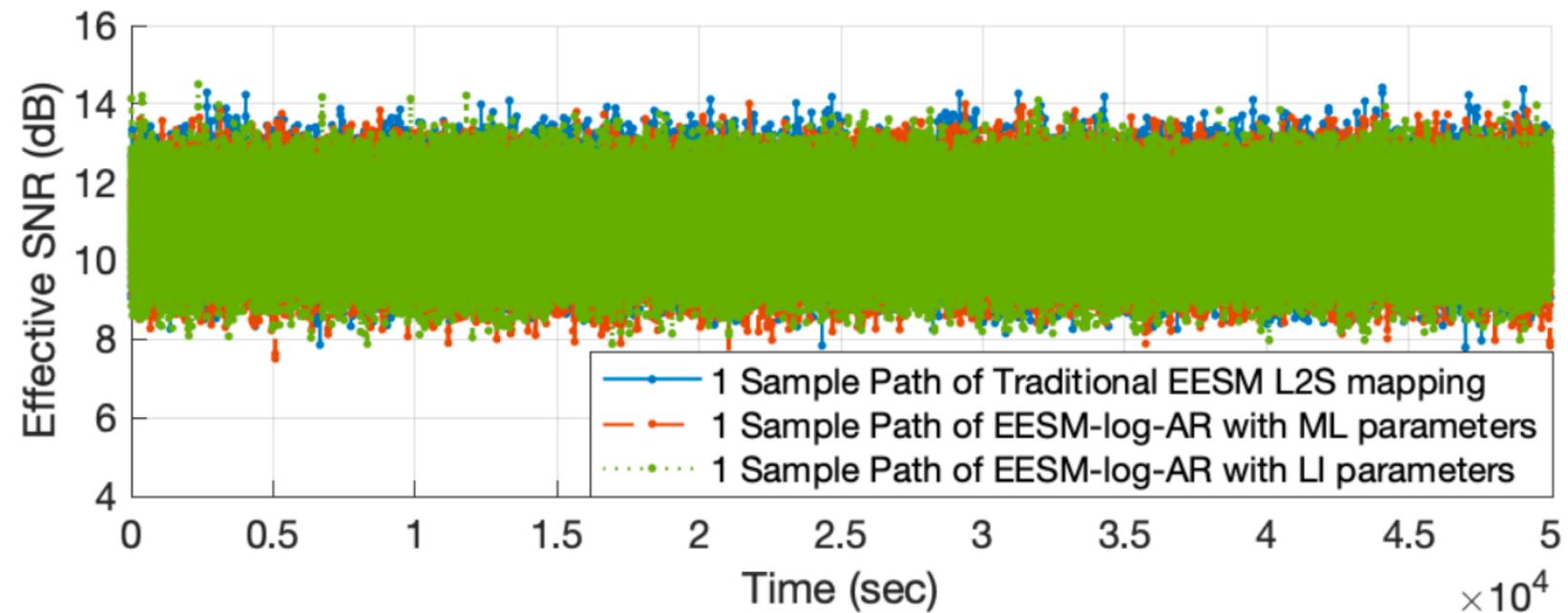
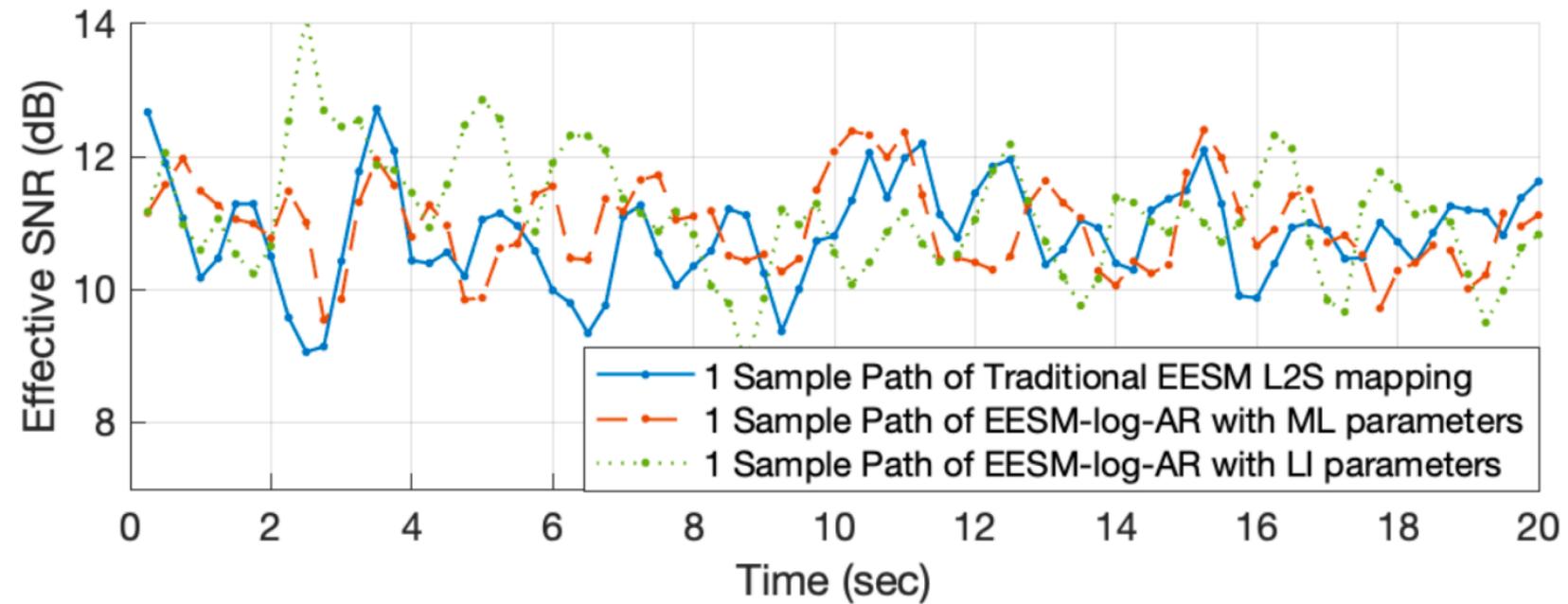
$$\hat{\sigma}_p^2(\gamma) = (1 - \epsilon)\hat{\sigma}_p^2(\gamma_1) + \epsilon\hat{\sigma}_p^2(\gamma_2)$$

$$\epsilon = \frac{\gamma - \gamma_1}{\gamma_2 - \gamma_1}$$

Estimated parameters

Stored parameters

Sample Paths of Effective SNR Processes



Residual Definition

- AR model

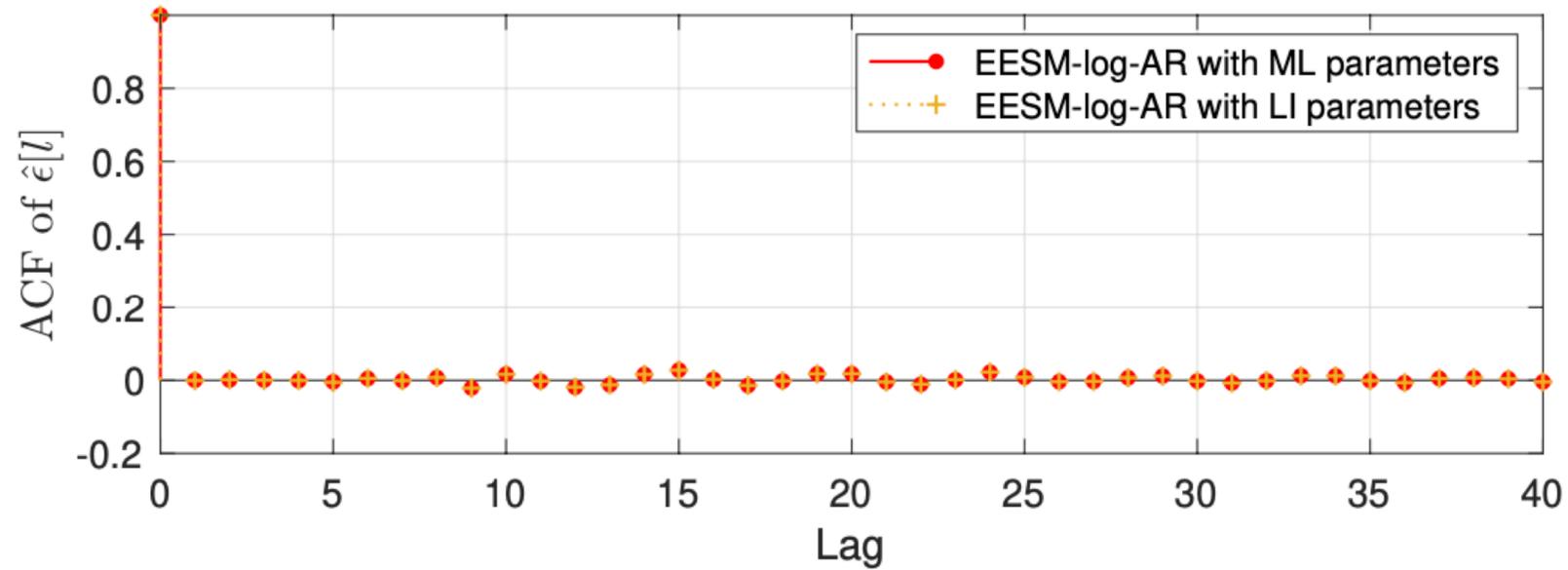
$$X[l] = c + \sum_{m=1}^p \phi_m X[l-m] + \epsilon[l]$$

zero-mean white Gaussian process
with a constant variance

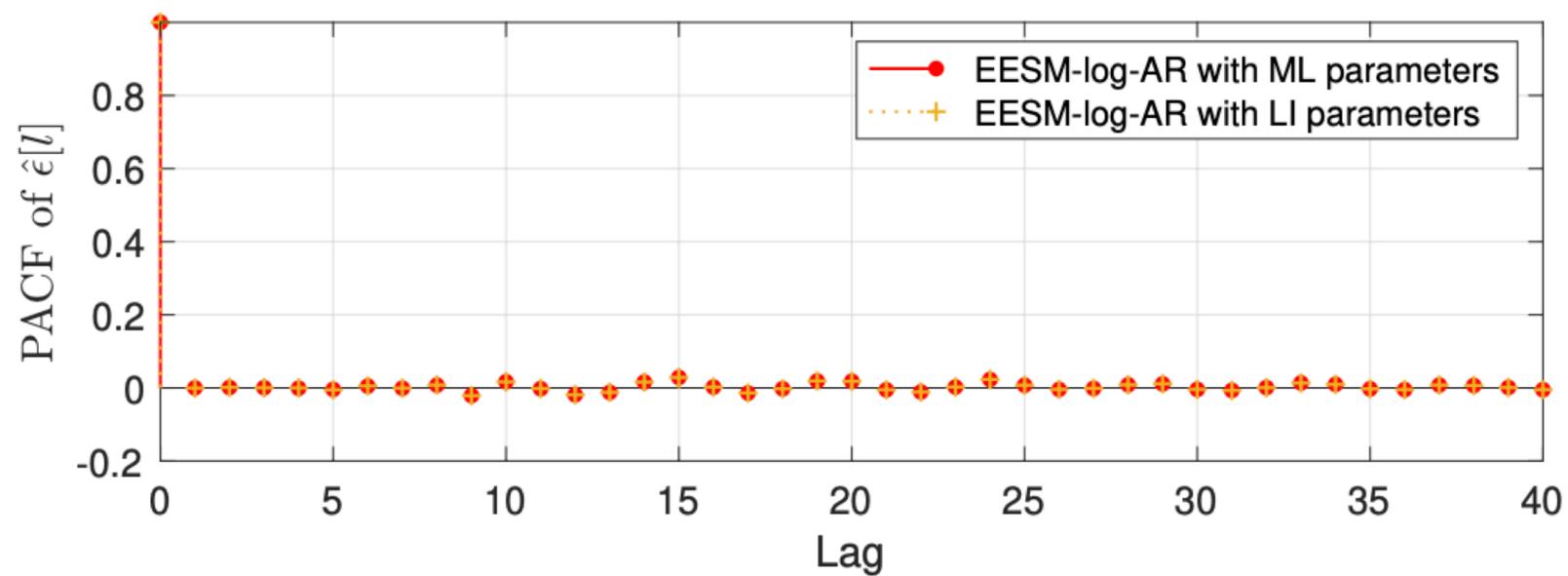
- Residual

$$\hat{\epsilon}[l] \triangleq X[l] - \hat{c}(\gamma) - \sum_{m=1}^p \hat{\phi}_m(\gamma) X[l-m]$$

Residual Whiteness Test



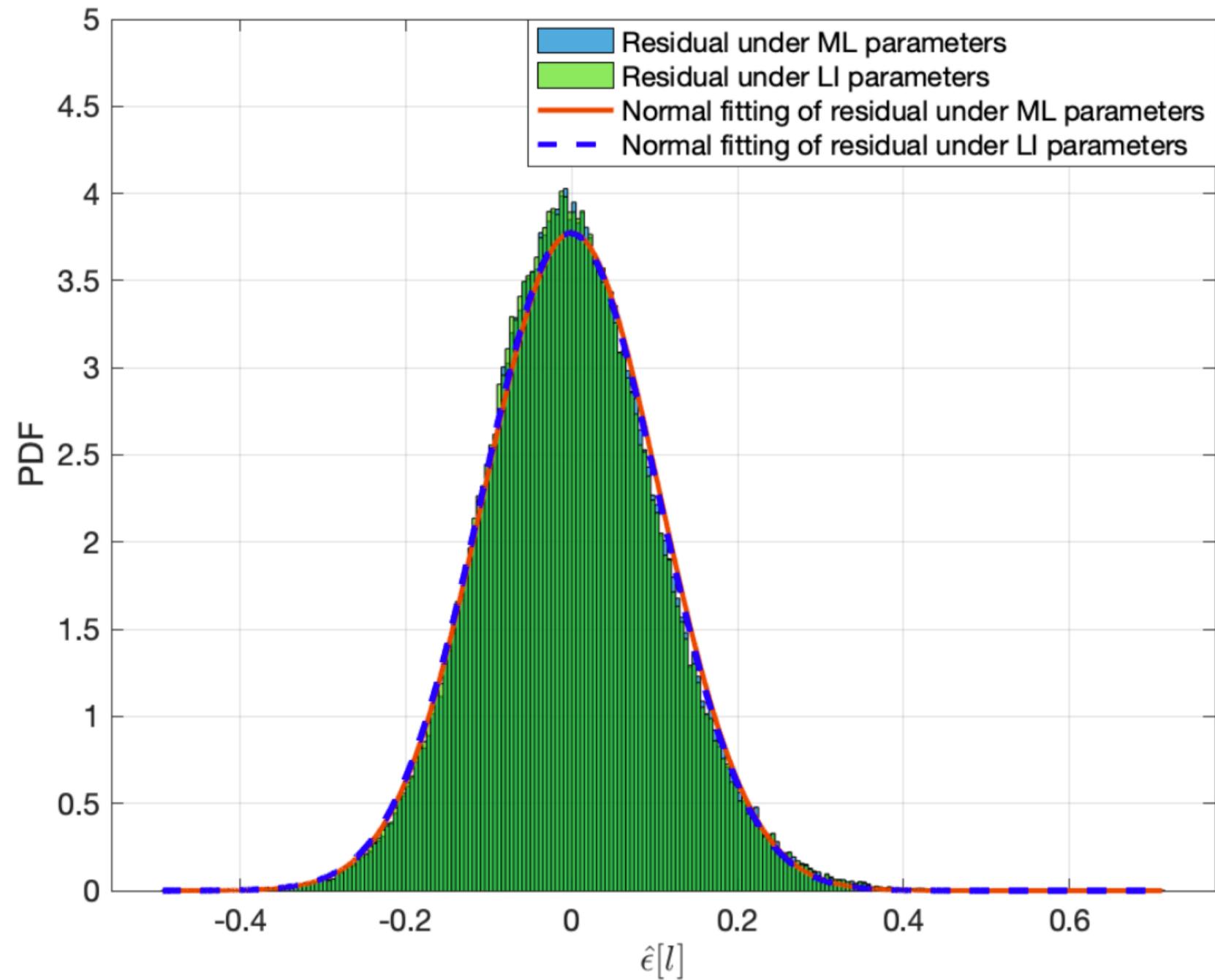
Check whether residual is white



Modified Leybourne- McCabe (LMC) Test

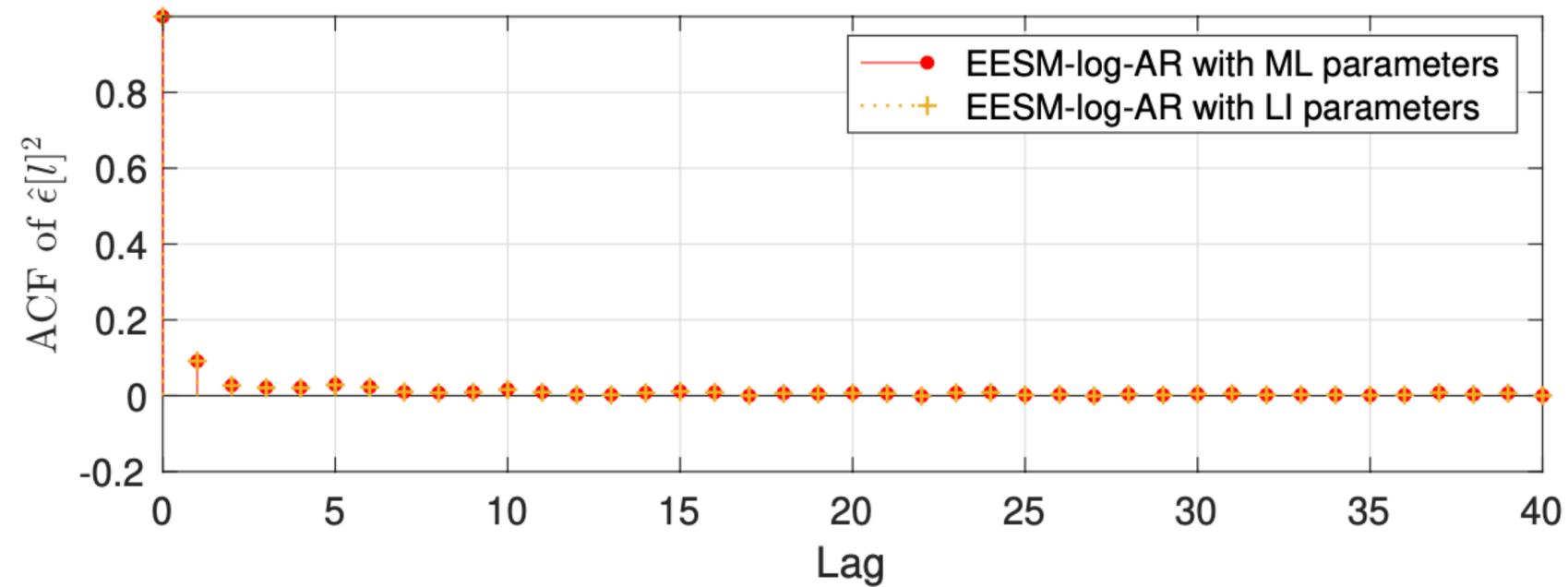
- Null hypothesis: $X [l]$ is a stationary $AR(p)$ process
- Our simulation: the modified LMC test fails to reject the null hypothesis with a large p-Value (> 0.05)
- Thus, $X [l]$ is stationary and can be modeled as an $AR(p)$ process

Residual Distribution

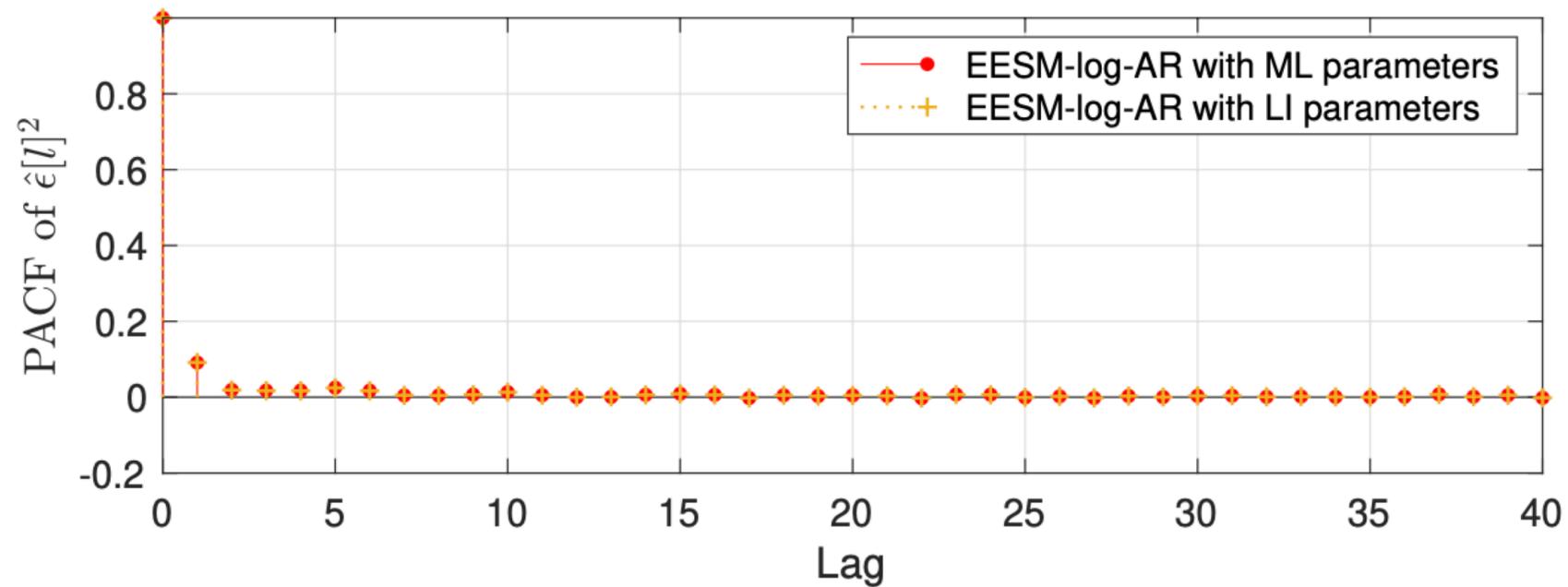


Check whether
residual \sim Gaussian
distribution

ACF and PACF of Squared Residual



Check whether
residual has
constant variance



Comparison

- EESM-log-SGN VS EESM-log-AR:
 - EESM-log-SGN model is more accurate for IID channel
 - EESM-log-AR has wider applicability as it is modeled for the general time-varying channel

Extension to 5G

- Inherent assumption for WiFi:
 - Slow fading (channel gain does not change in a packet duration)
 - No inter-carrier interference or ICI (extreme low Doppler)
- Extension to 5G
 - Fast fading
 - ICI introduced by Doppler

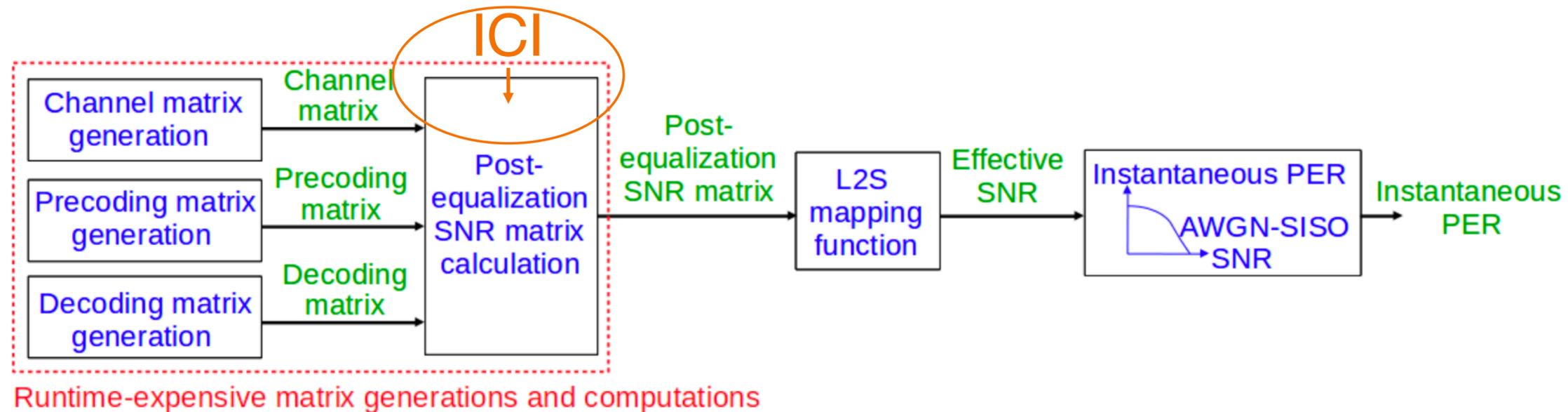
Extension to 5G

- Fast fading

Channel gain



- Consider ICI



Interference Scenario

